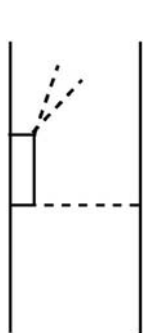


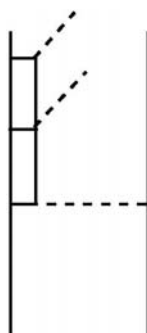
*Two pion production in  $pp \rightarrow pp\pi\pi$  -  
do we see a sign of  $\Delta(1600)$  excitation?*

**T. Skorodko, University Tuebingen  
for CELSIUS-WASA**

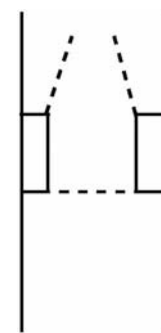
- ▶ experiment  $\leftrightarrow$  theory
- ▶ isospin decomposition
- ▶ conclusions



$$N^* \rightarrow N\sigma$$

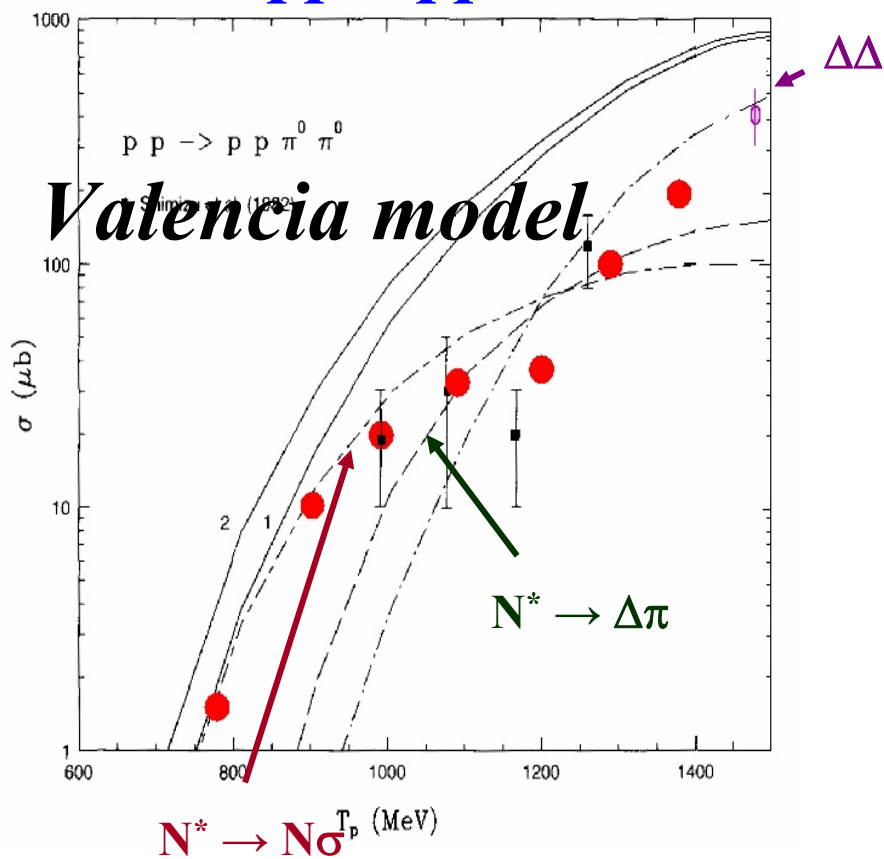


$$N^* \rightarrow \Delta\pi$$

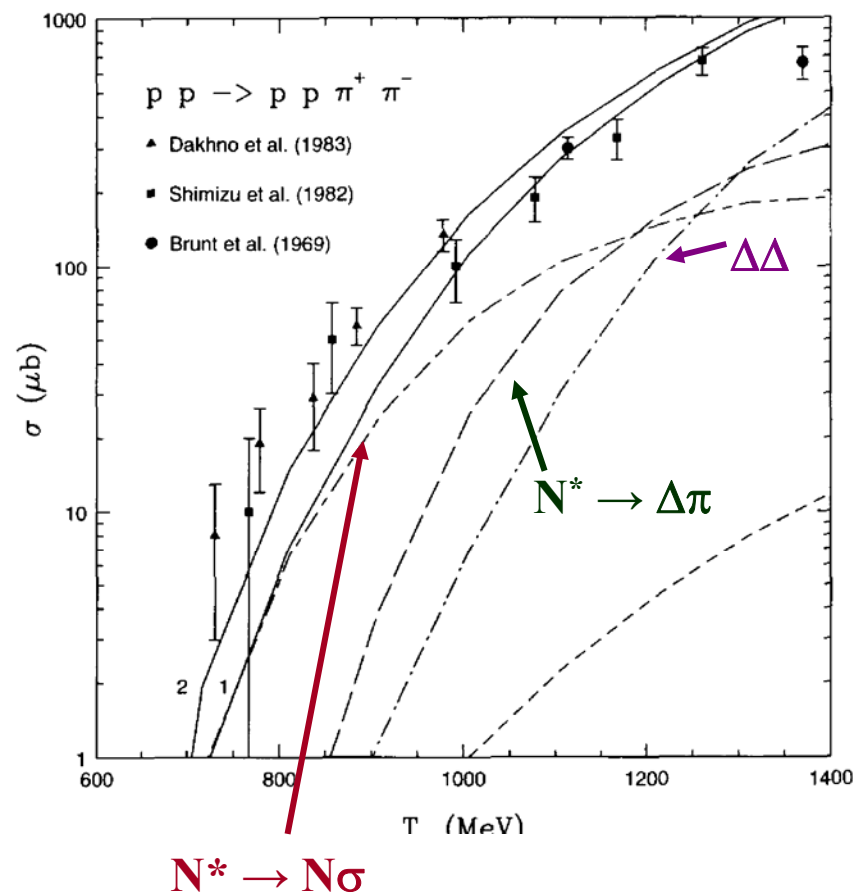


$$\Delta\Delta$$

$$pp \rightarrow pp\pi^0\pi^0$$

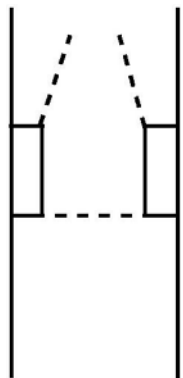


$$pp \rightarrow pp\pi^+\pi^-$$

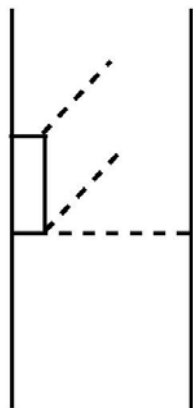


# Total cross section

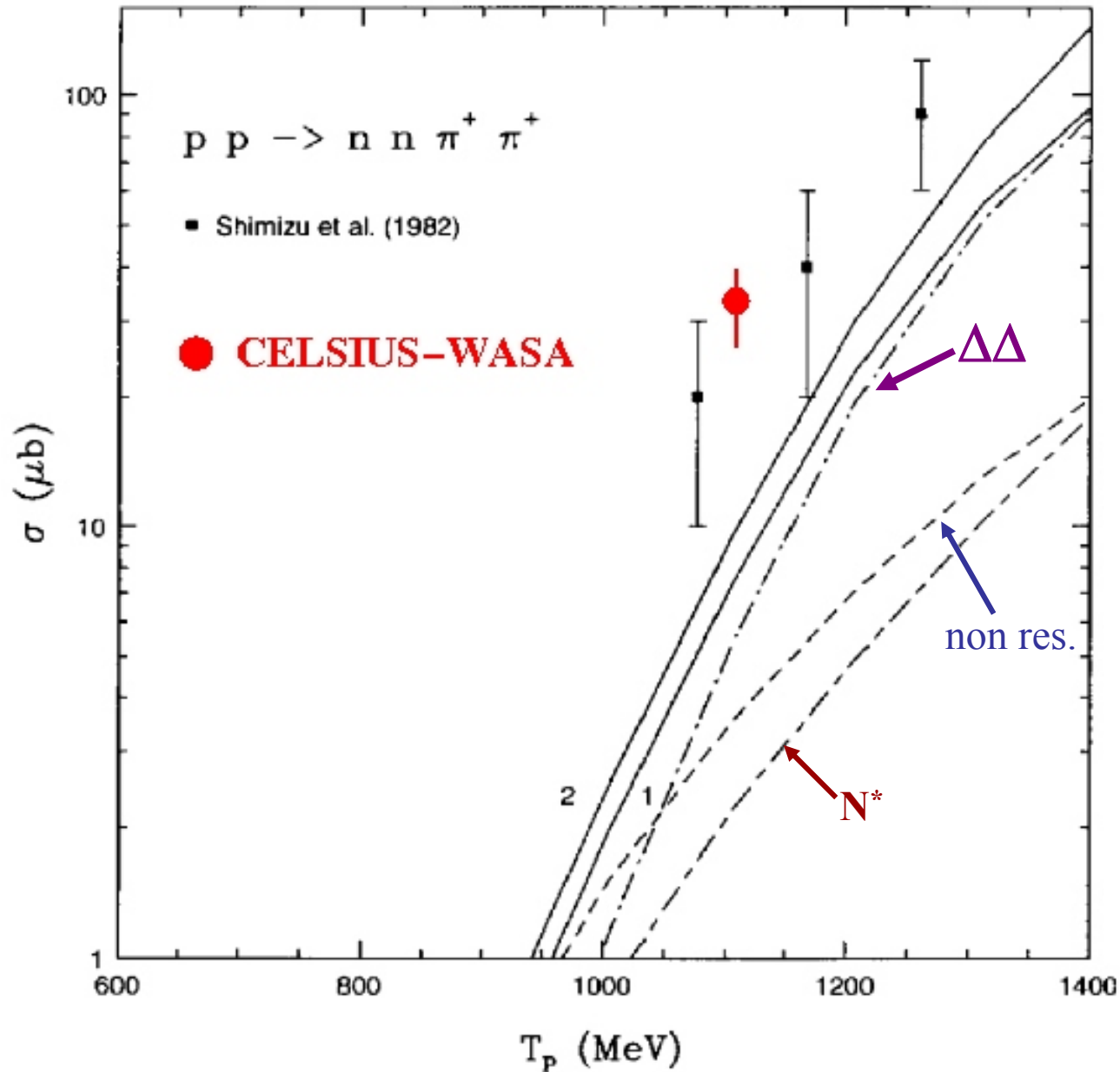
$$pp \rightarrow nn \pi^+ \pi^+$$



$\Delta\Delta$



$N^*$



# Isospin decomposition

$$M_{(I_{NN})_f I_{\pi\pi} (I_{NN})_i}$$

$$\sigma_{nn\pi^+\pi^+} = \frac{3}{20} |M_{121}|^2$$

$$\sigma_{pp\pi^0\pi^0} = \frac{1}{60} |M_{121} - \sqrt{5}M_{101}|^2 =$$

$$\frac{1}{60} |M_{121}|^2 + \frac{1}{12} |M_{101}|^2 - \frac{1}{\sqrt{180}} |M_{121}| |M_{101}| \cos\varphi$$

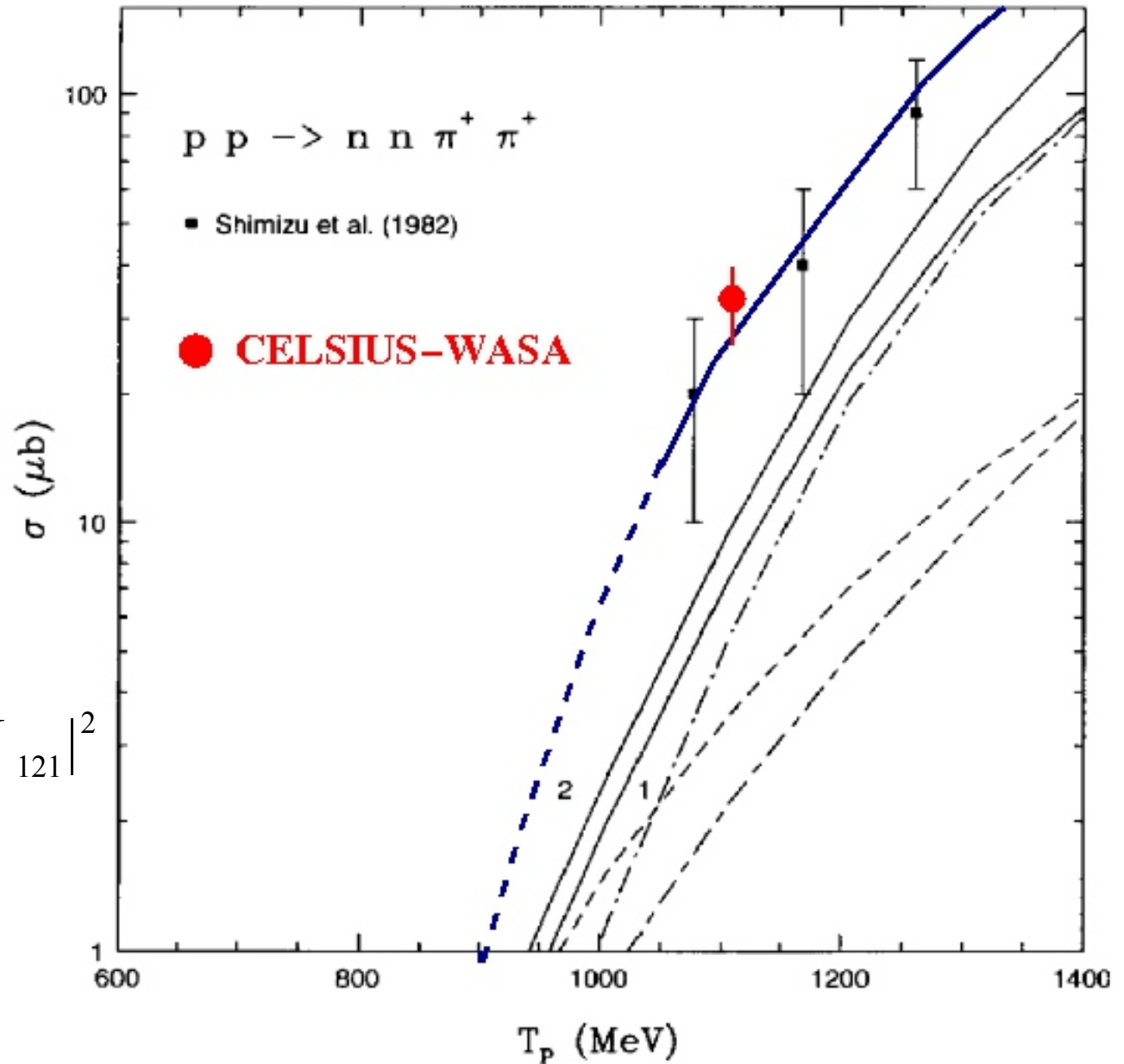
$$\sigma_{pp\pi^-\pi^+} = \frac{1}{120} |M_{121} + 2\sqrt{5}M_{101}|^2 + \frac{1}{8} |M_{111}|^2 =$$

$$|M_{111}|^2 + \frac{1}{120} |M_{121}|^2 + \frac{1}{6} |M_{101}|^2 + \frac{1}{\sqrt{180}} |M_{121}| |M_{101}| \cos\varphi$$

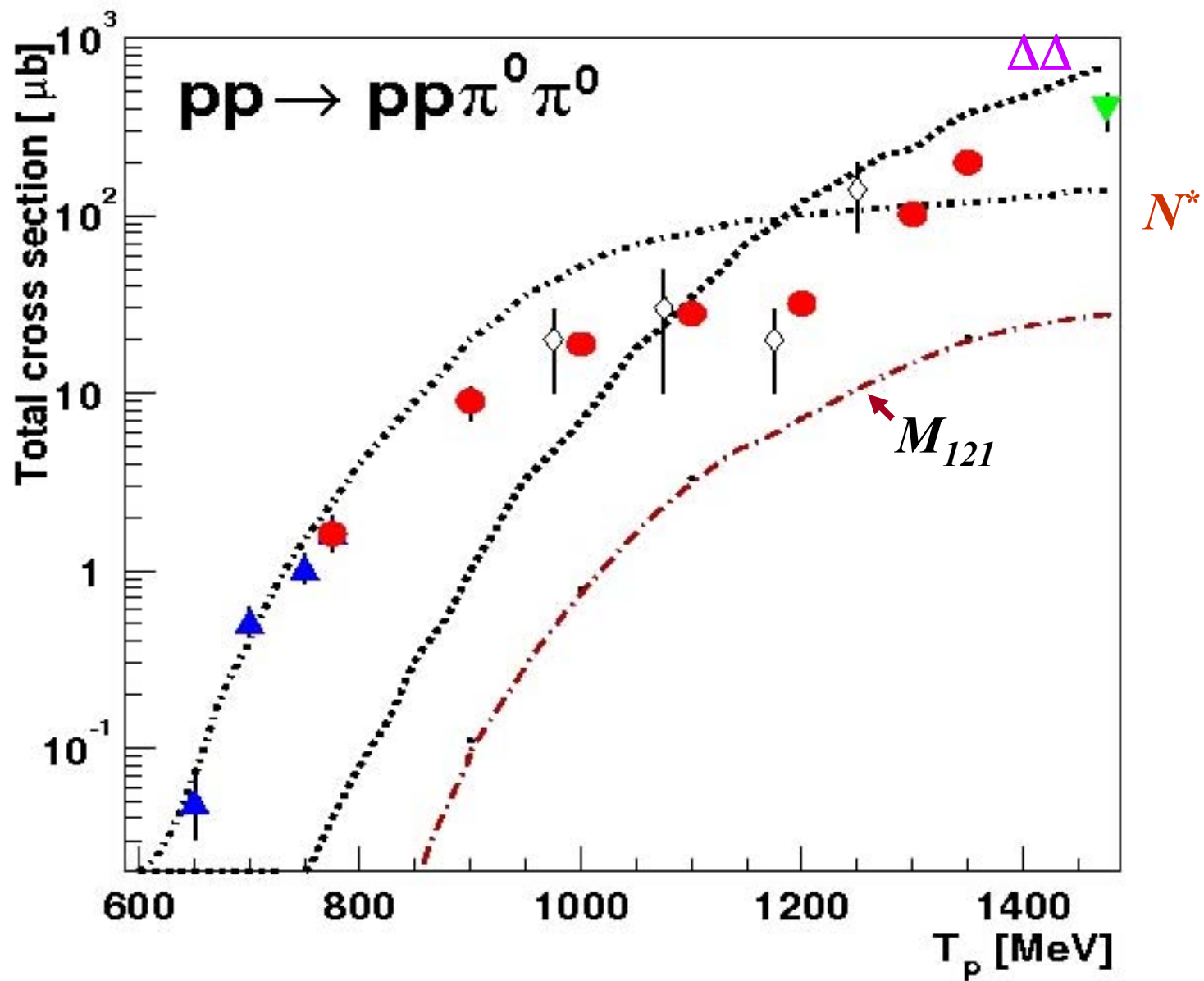
# Total cross section

$$pp \rightarrow nn \pi^+ \pi^+$$

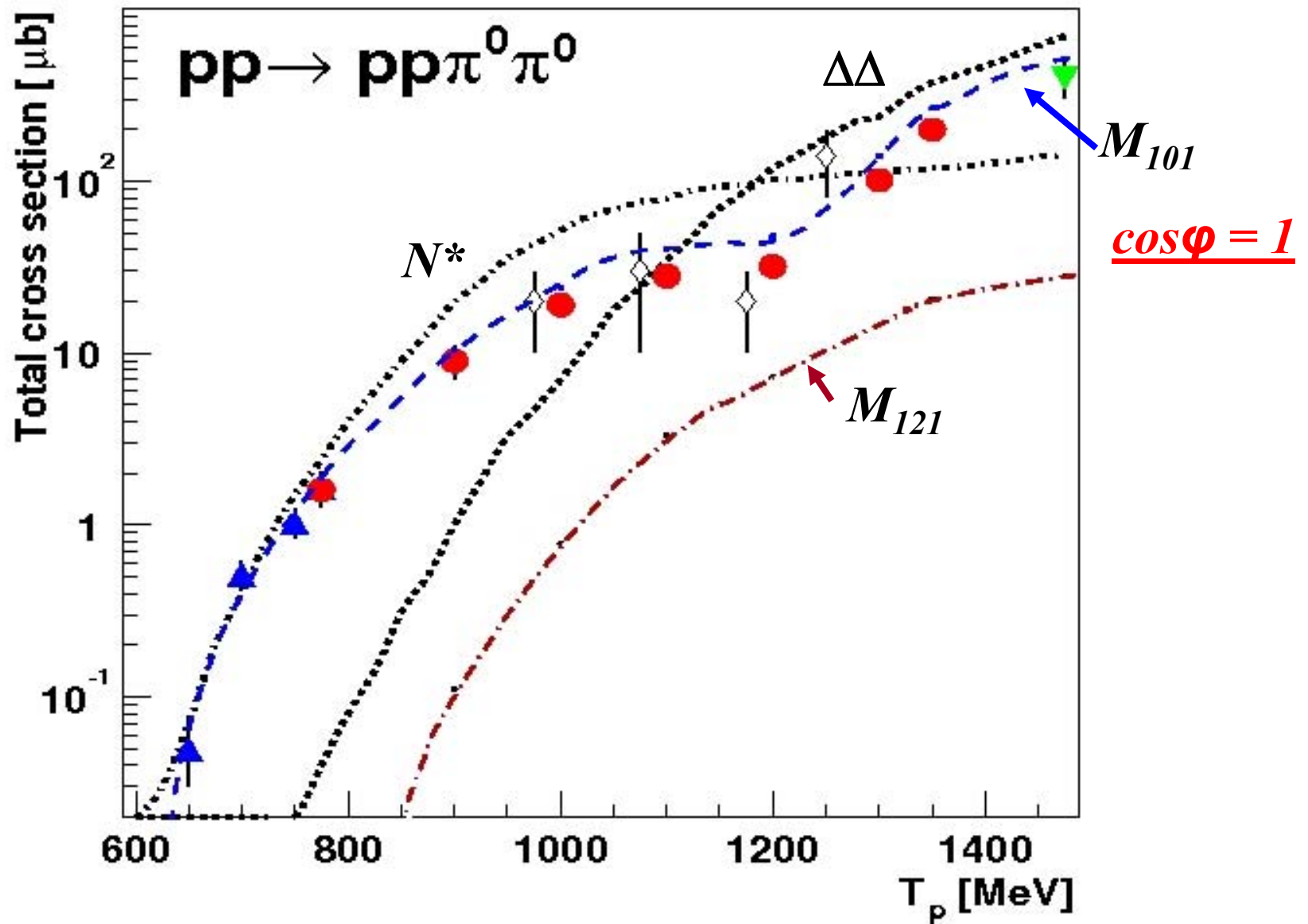
$$\sigma_{pp \pi^+ \pi^+} = \frac{3}{20} |M_{121}|^2$$



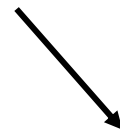
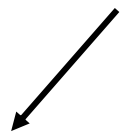
# Total cross section



# Total cross section

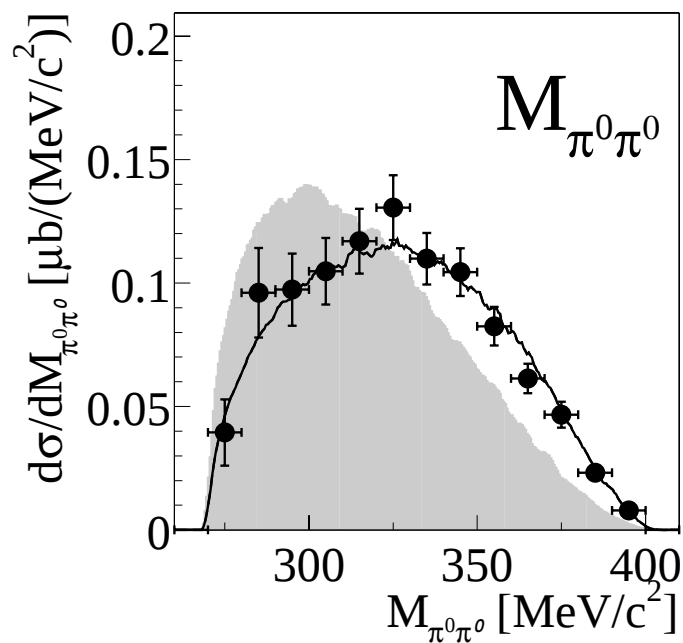


$$|M_{101}| = |M_{101}^{N^*} + M_{101}^{\Delta\Delta}|$$

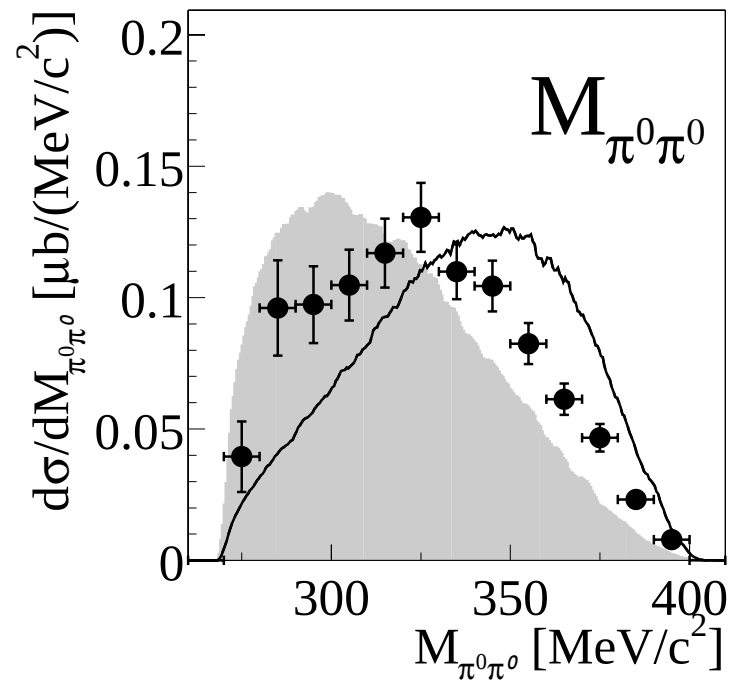


$$|M_{101}^{N^*}| = |M_{101}| - |M_{101}^{\Delta\Delta}|$$

$$|M_{101}^{N^*}| = |M_{101}| + |M_{101}^{\Delta\Delta}|$$

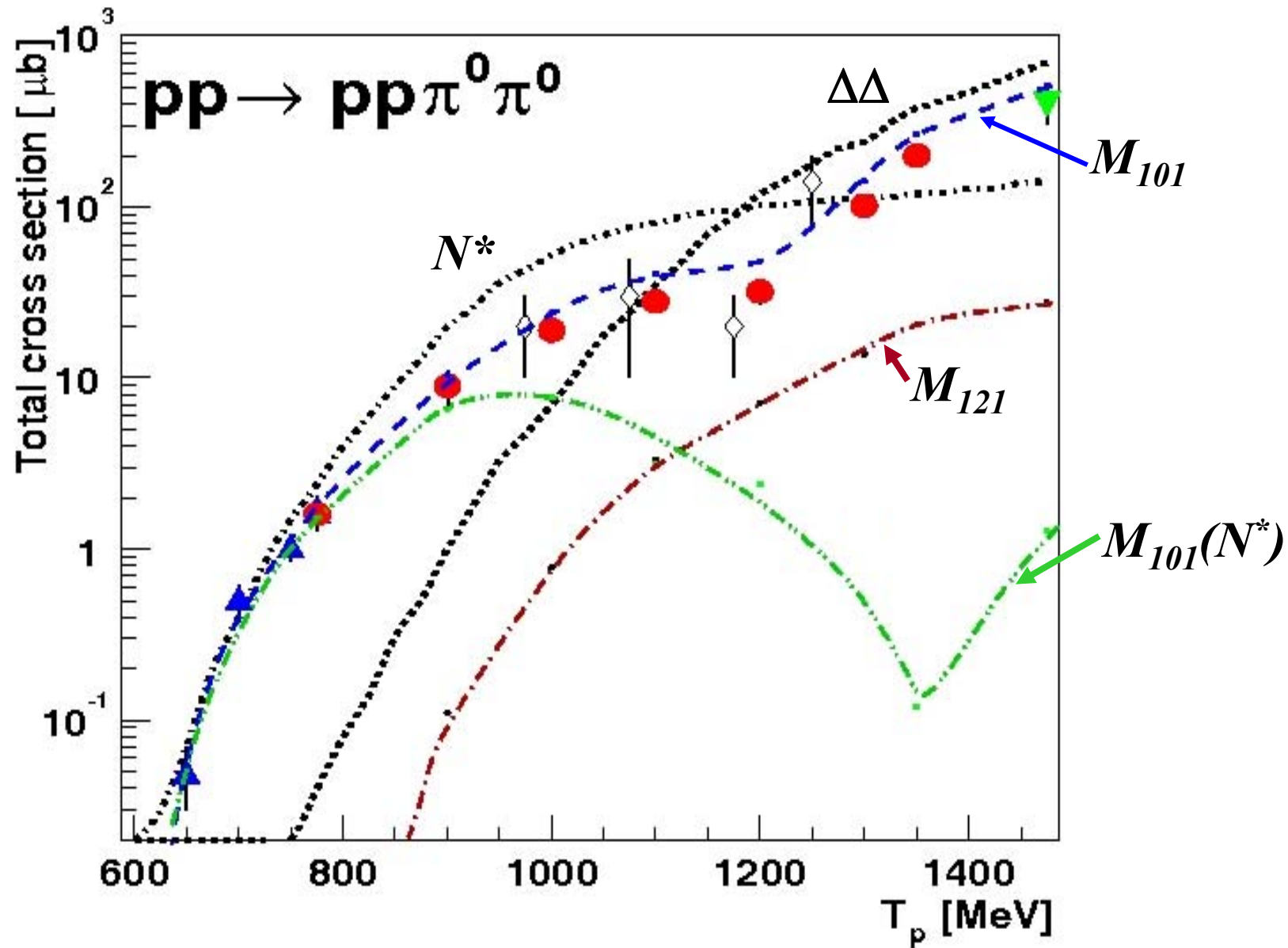


$T_p = 900 \text{ MeV}$



$$M_{101}^{N^*} = M_{101} - M_{101}^{\Delta\Delta}$$

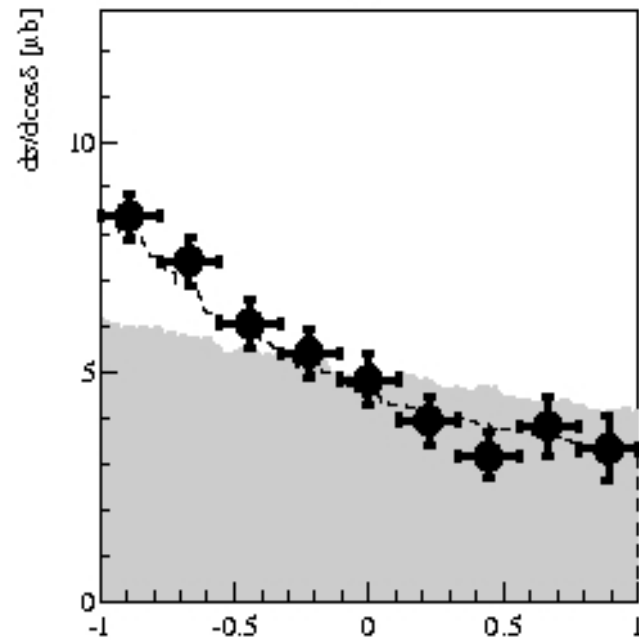
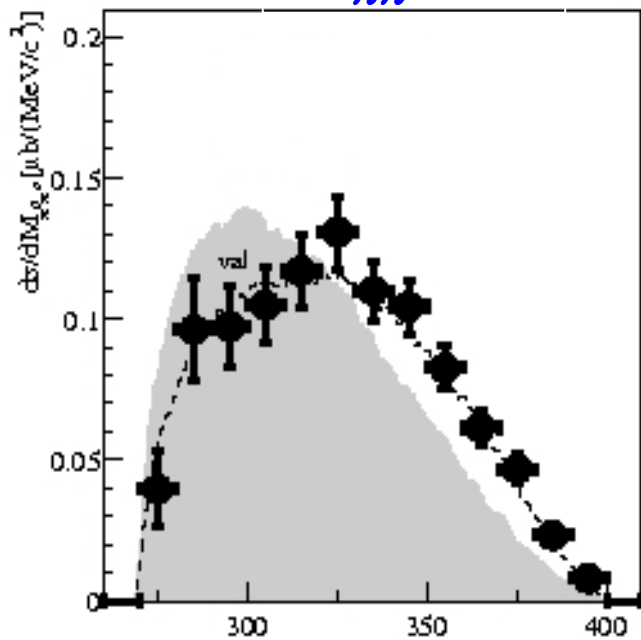
# Total cross section



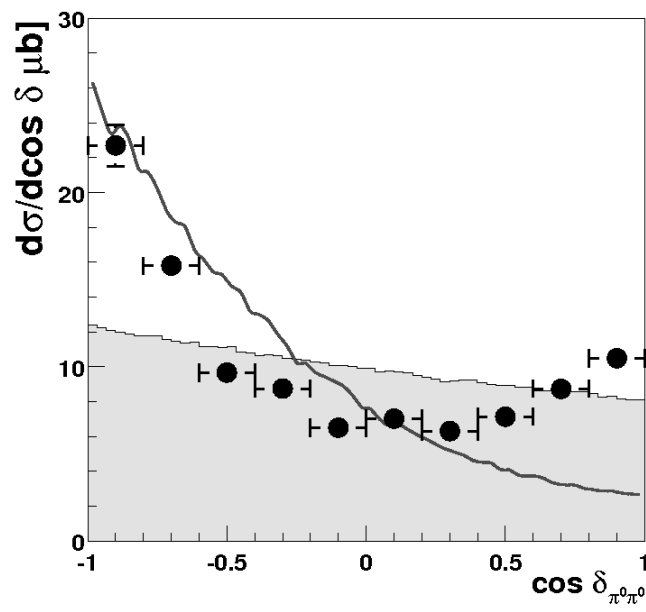
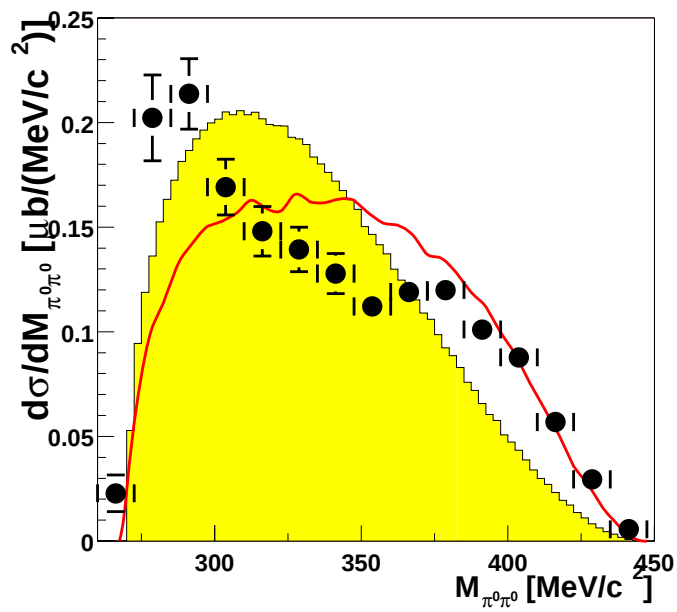
$$\underline{pp \rightarrow pp \pi^0 \pi^0}$$

$$M_{\pi\pi}$$

$$\delta_{\pi\pi}$$



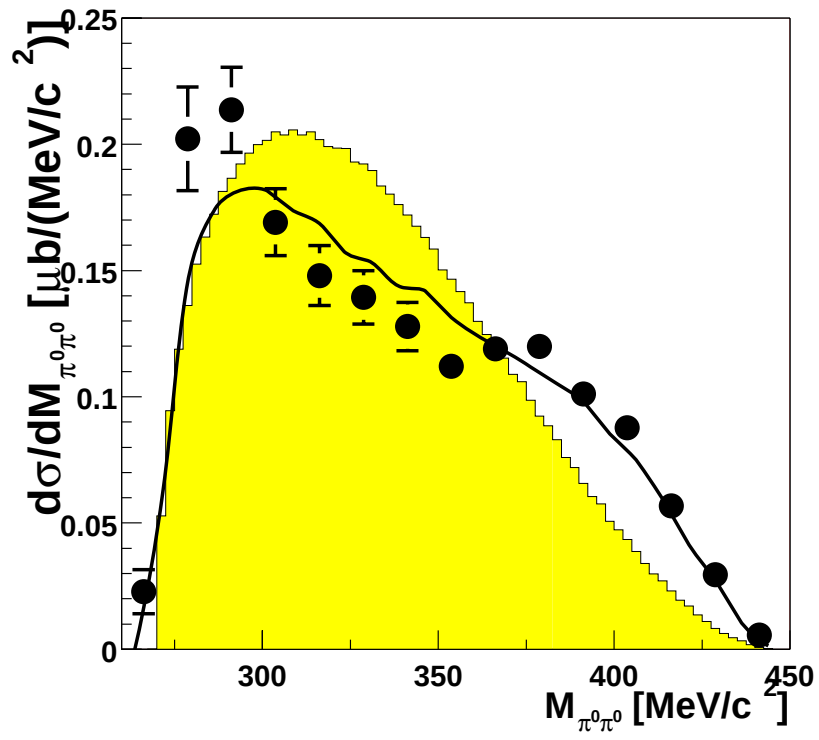
$$T_p = 895 \text{ MeV}$$



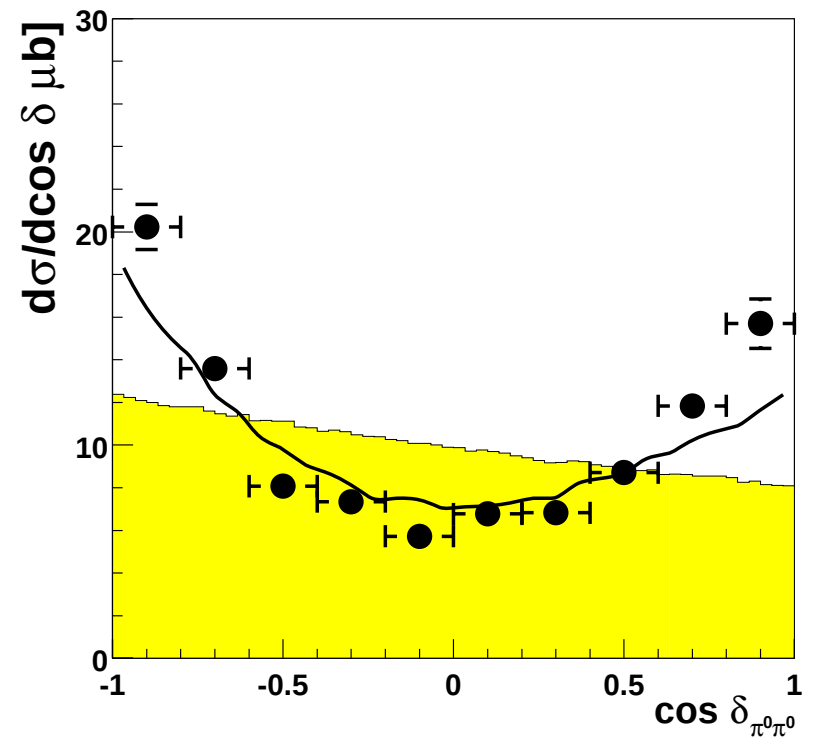
$$T_p = 1000 \text{ MeV}$$

$$pp \rightarrow pp \pi^0 \pi^0 \quad T_p = 1000 \text{ MeV.}$$

$M_{\pi\pi}$

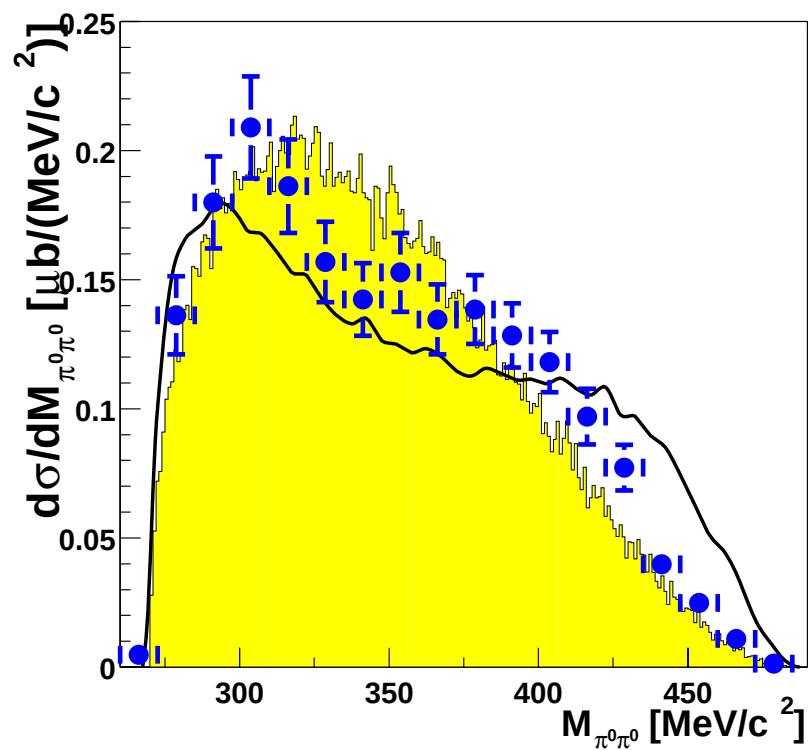


$\delta_{\pi\pi}$

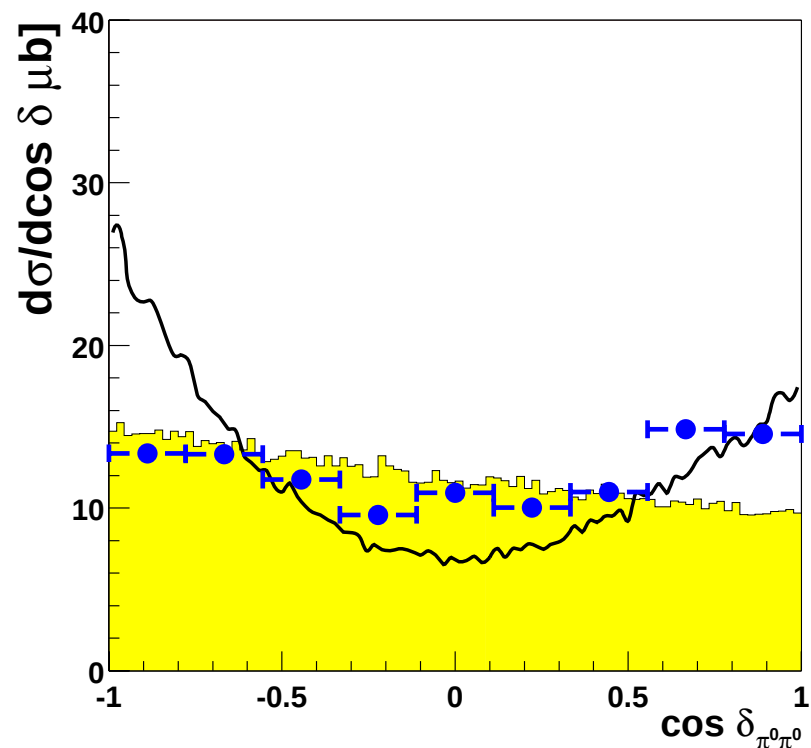


$$pp \rightarrow pp \pi^0 \pi^0 \quad T_p = 1100 \text{ MeV}.$$

$M_{\pi\pi}$

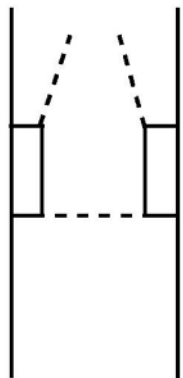


$\delta_{\pi\pi}$

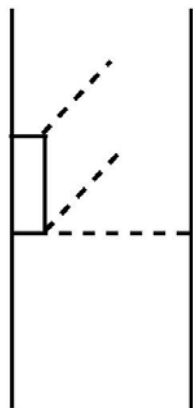


# Total cross section

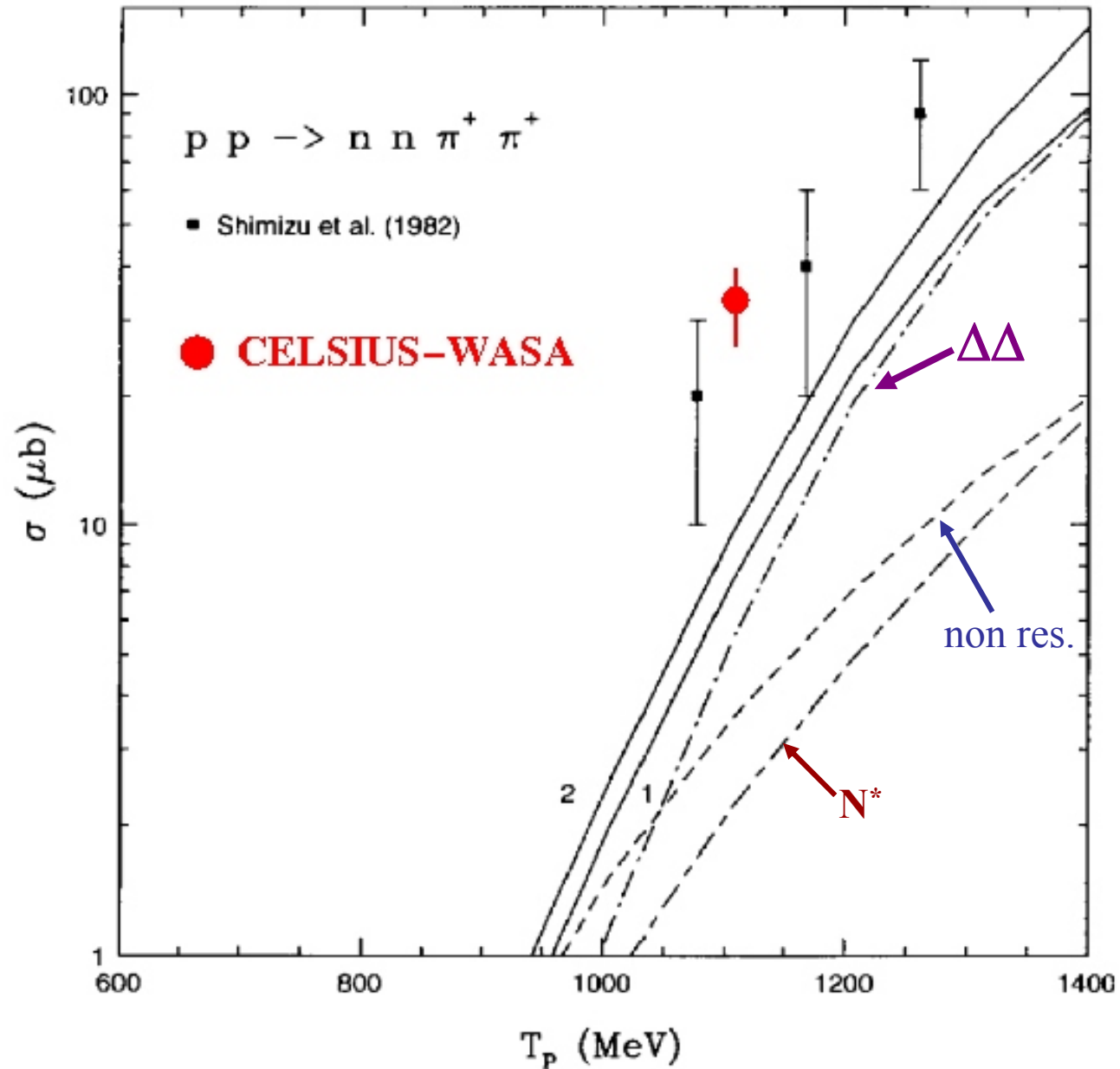
$$pp \rightarrow nn \pi^+ \pi^+$$



$\Delta\Delta$



$N^*$



$$\mathbf{M}_{121}$$

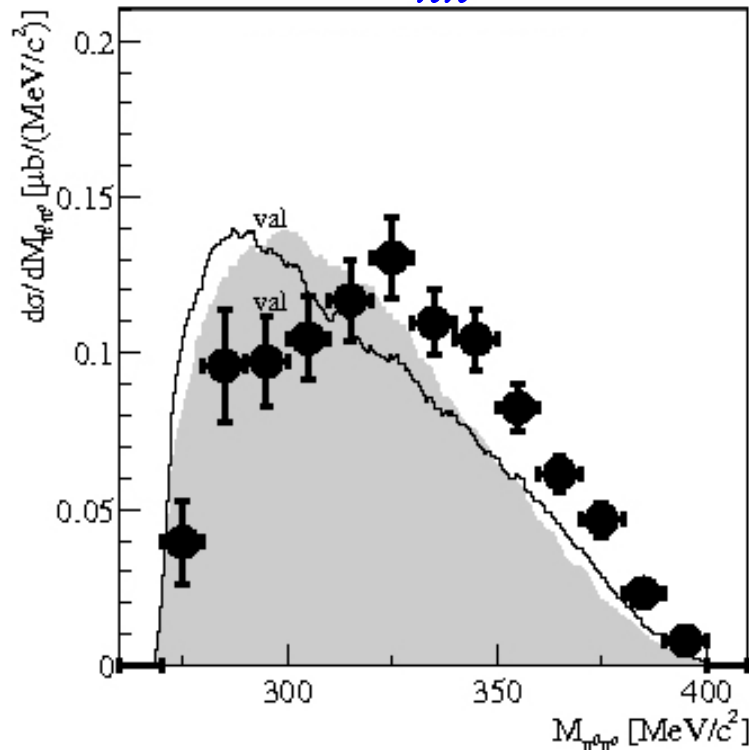
$$M_{121} = M_{121}^{\Delta\Delta}$$

 $\Rightarrow$ 

in 4 times bigger  $\Delta\Delta$  cross section in  $pp\pi^0\pi^0$

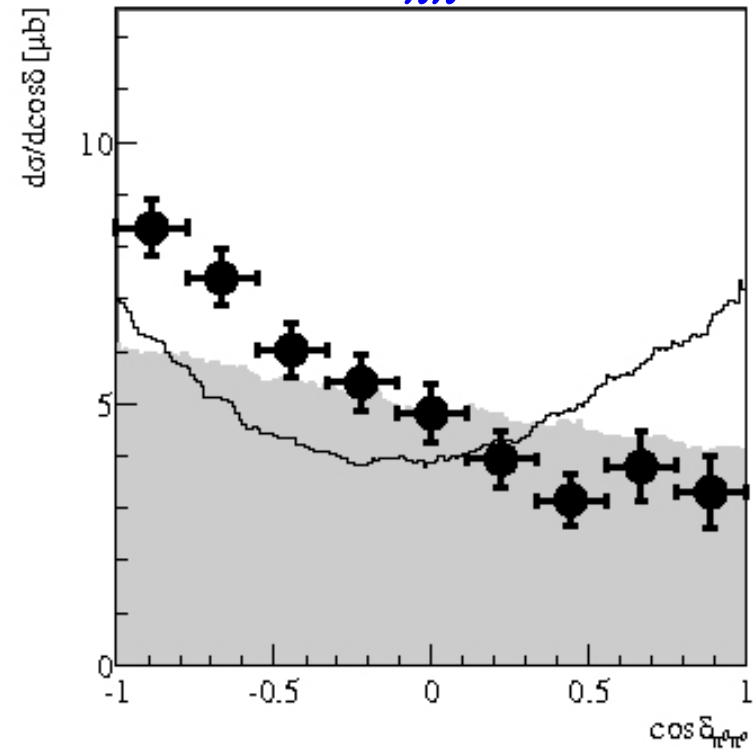
$$M_{101}^{\Delta\Delta} = -\sqrt{5}M_{121}^{\Delta\Delta}$$

$M_{\pi\pi}$



$\delta_{\pi\pi}$

$T_p = 900 \text{ MeV}$



$$\boxed{\mathbf{M}_{121}}$$

~~$$M_{121} = M_{121}^{\Delta\Delta}$$~~

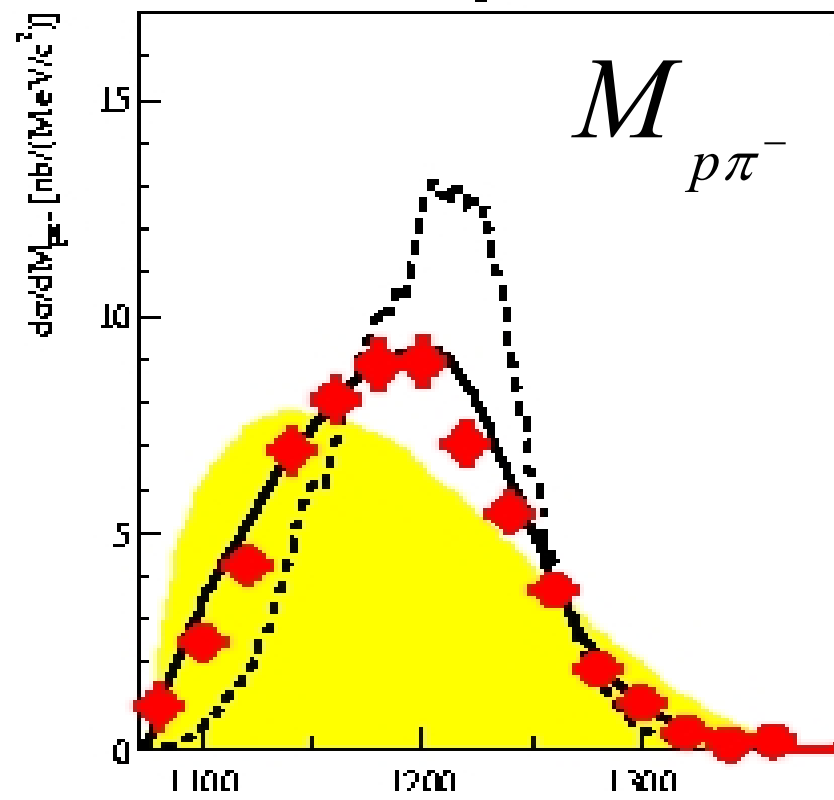
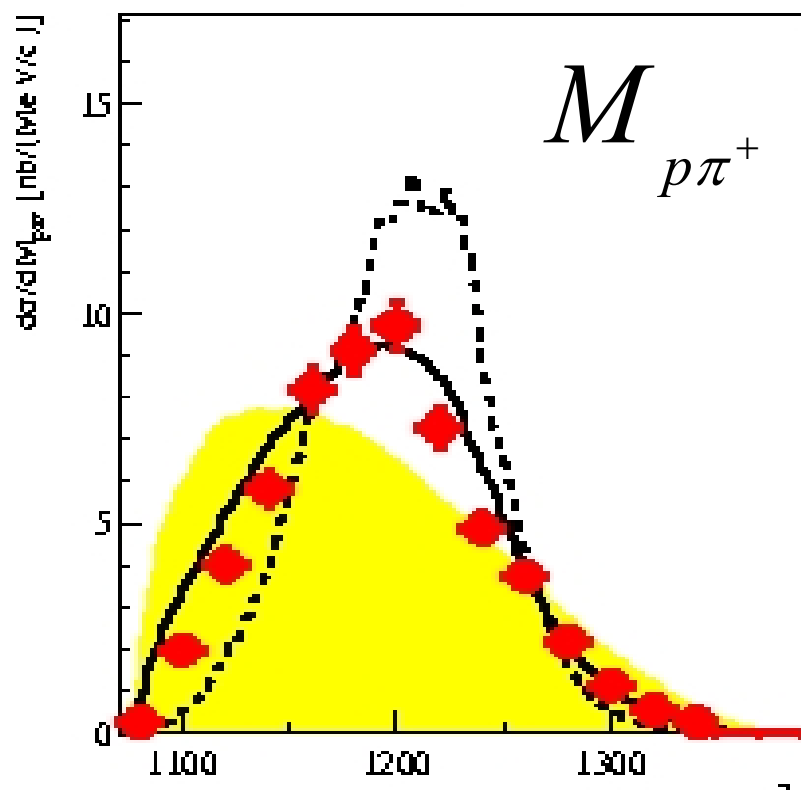
 $\Rightarrow$ 

in 4 times bigger  $\Delta\Delta$  cross section in  $pp\pi^0\pi^0$

$$|M_{121}| = \left| \sum M_{121}^{I=\frac{3}{2}} \right| \Rightarrow$$

no contribution from  $\Delta\Delta$

$$pp \rightarrow pp \pi^+ \pi^- \quad T_p = 1360$$



$$\boxed{\mathbf{M}_{121}}$$

~~$$M_{121} = M_{121}^{\Delta\Delta} \Rightarrow \text{in 4 times bigger } \Delta\Delta \text{ cross section in } pp\pi^0\pi^0$$~~

~~$$|M_{121}| = \left| \sum M_{121}^{I=\frac{3}{2}} \right| \Rightarrow \text{no contribution from } \Delta\Delta$$~~

$$|M_{121}| = \left| M_{121}^{\Delta\Delta} + \sum M_{121}^{I=\frac{3}{2}} \right|$$

$$\mathbf{M}_{121}$$

$$|M_{121}| = |M_{121}^{\Delta\Delta} + \sum M_{121}^{I=\frac{3}{2}}|$$

$\Delta(1232)$

$\Delta(1600)$

*very small amplitude*

*according to Valencia model*

$M_{\Delta}=1500-1700 \text{ MeV} \Rightarrow$

*threshold energy  $\approx$  threshold energy  $\Delta\Delta$*

$\Gamma_{\Delta}=200-400 \text{ MeV} \Rightarrow$

*can contribute at low energy*

$$\left| M_{121} \right| = \left| M_{121}^{\Delta\Delta} + M_{121}^{\Delta_{1600}} \right|$$

~~$$\left| M_{121} \right| = \left| M_{121}^{\Delta_{1600}} \right| + \left| M_{121}^{\Delta\Delta} \right|$$~~

$$\cos\varphi \approx +1$$

$$\left| M_{121} \right| = \left| M_{121}^{\Delta_{1600}} \right| - \left| M_{121}^{\Delta\Delta} \right|$$



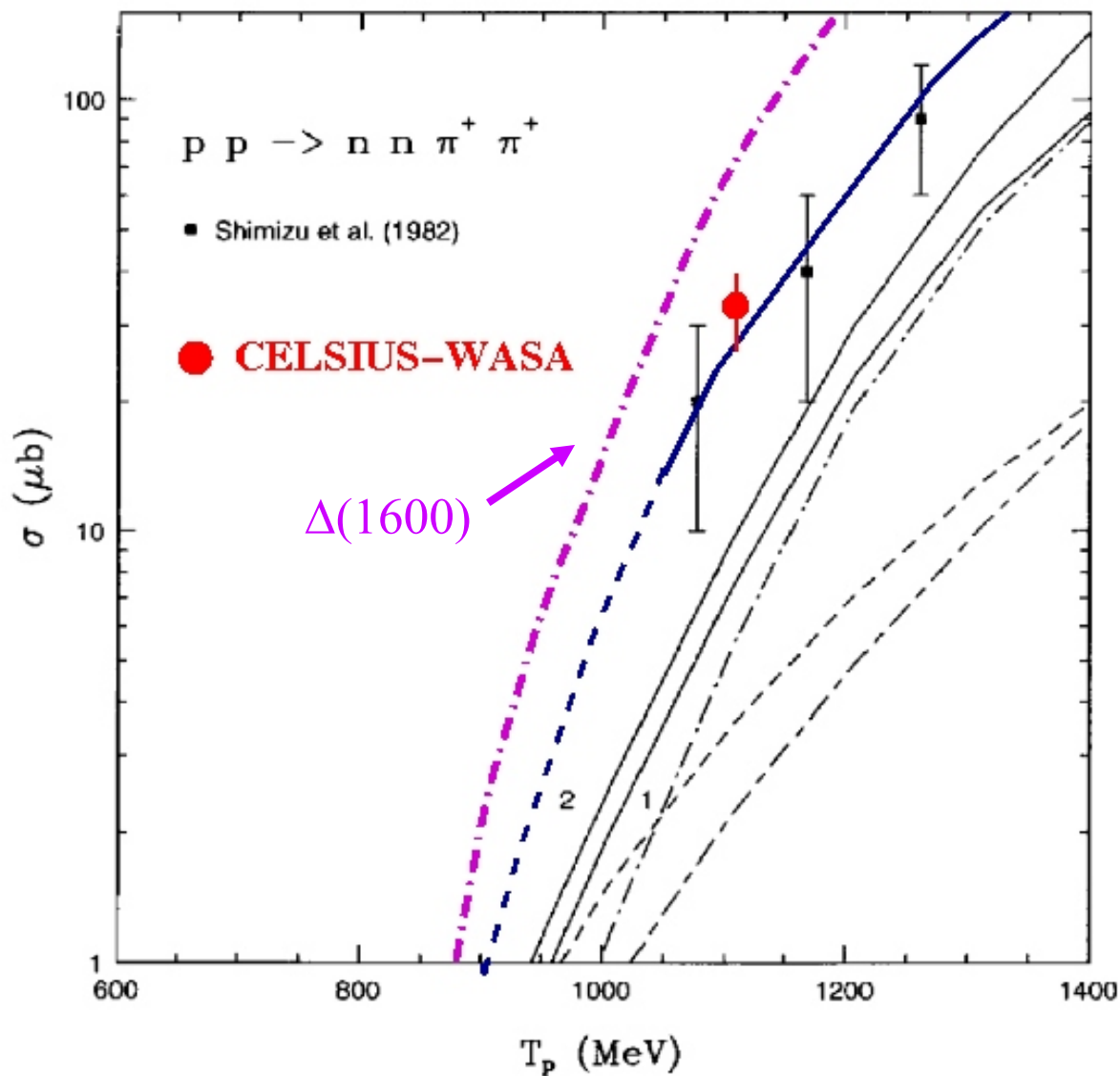
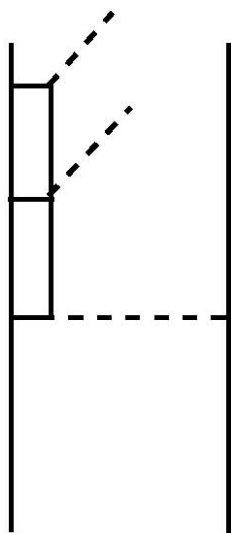
$$M_{101}^{\Delta\Delta} = -\sqrt{5} M_{121}^{\Delta\Delta}$$

# Total cross section

$$pp \rightarrow nn \pi^+ \pi^+$$

$\Delta(1232)$

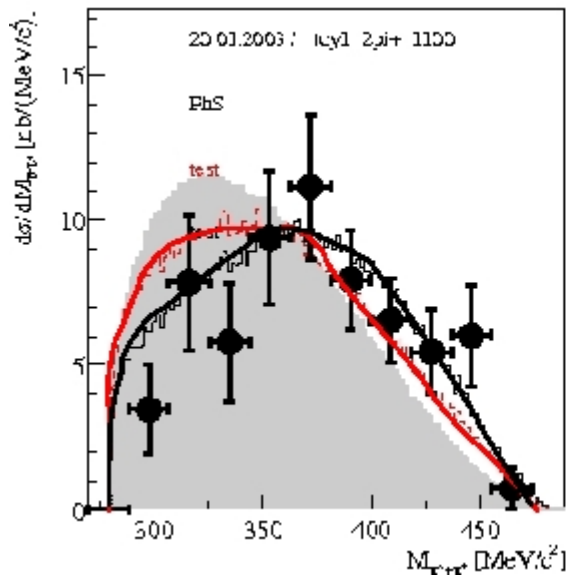
$\Delta(1600)$



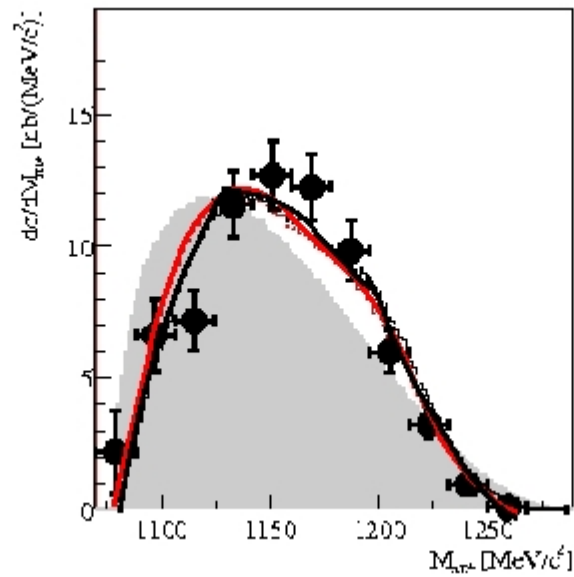
$$pp \rightarrow nn \pi^+ \pi^+$$

$$T_p = 1100 \text{ MeV}$$

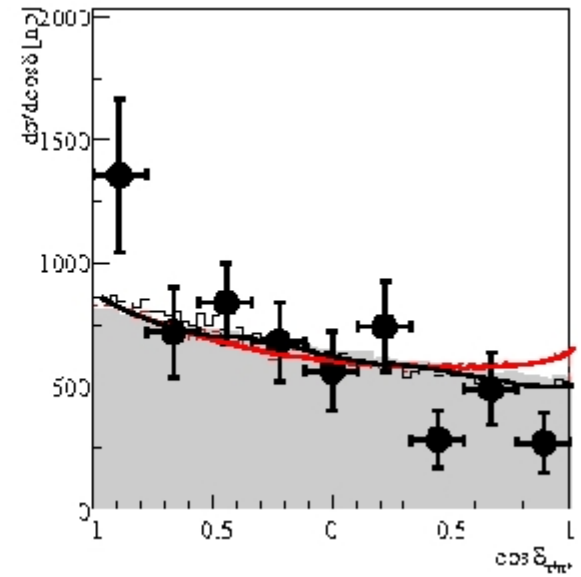
$$M_{\pi\pi}$$



$$M_{n\pi}$$



$$\delta_{\pi\pi}$$



—  $\Delta(1600)$

—  $\Delta(1232)$

# Conclusions

- contribution from particle with spin 3/2 should be added in model description

$\Delta(1600)$  – possible candidate

- $pp \rightarrow pn\pi^0\pi^+$

