

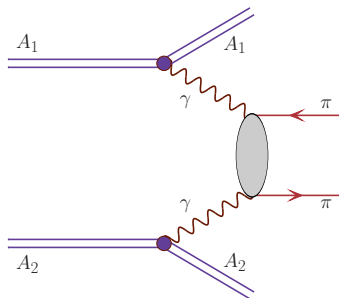


Institute of Nuclear Physics PAN, PL-31-342 Cracow, Poland

Exclusive production of $\pi^+\pi^-$ and $\pi^0\pi^0$ pairs
in photon-photon and in ultrarelativistic
heavy ion collisions

Mariola Kłusek-Gawenda

In collaboration with prof. A. Szczurek



Accelerator LHC:

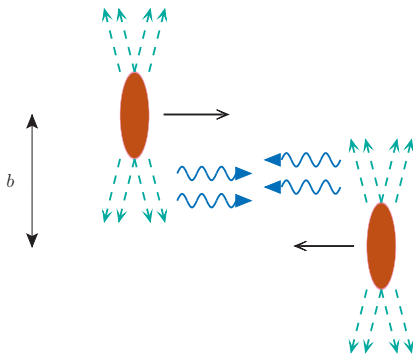
- nuclei: Pb-Pb
- $\sqrt{s_{NN}} = 3.5 \text{ TeV}$
- $\gamma_{cm} = 2\,932 \text{ GeV}$

$$PbPb \rightarrow PbPb\pi^0\pi^0$$

$$PbPb \rightarrow PbPb\pi^+\pi^-$$

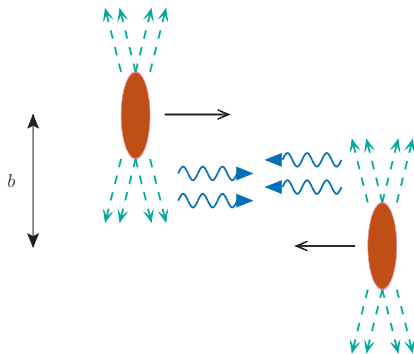
- 1 Equivalent photon approximation
 - Form factor
 - Realistic
 - Monopole
- 2 $\gamma\gamma \rightarrow \pi\pi$
 - dipion continuum
 - $\gamma\gamma \rightarrow$ resonances
 - pion-pion rescatterings
 - $\rho^\pm$ exchange
 - pQCD
- 3 Nuclear cross section
- 4 Conclusions

Equivalent photon approximation (EPA)



The strong electromagnetic field is used as a source of photons to induce electromagnetic reactions.

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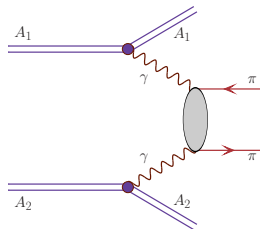
Peripheral collisions:

$$b > R_1 + R_2 \cong 14 \text{ fm}$$

The total cross section in EPA

$$\sigma(PbPb \rightarrow PbPb\pi\pi; s_{NN})$$

$$= \int \hat{\sigma}(\gamma\gamma \rightarrow \pi\pi; x_1 x_2 s_{NN}) dn_{\gamma\gamma}(x_1, x_2, \mathbf{b})$$

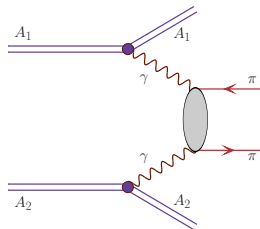


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- $x_{1,2} = \frac{\omega_{1,2}}{\gamma M_A}$



Photons flux

$$dn_{\gamma\gamma}(x_1, x_2, \mathbf{b}) = \int \frac{1}{\pi} d^2\mathbf{b}_1 |\mathbf{E}(x_1, \mathbf{b}_1)|^2 \frac{1}{\pi} d^2\mathbf{b}_2 |\mathbf{E}(x_2, \mathbf{b}_2)|^2 \\ \times S_{abs}^2(\mathbf{b}) \delta^{(2)}(\mathbf{b} - \mathbf{b}_1 + \mathbf{b}_2) \frac{dx_1}{x_1} \frac{dx_2}{x_2}$$

- $\mathbf{E}(x, \mathbf{b}) = Z \sqrt{4\pi\alpha_{em}} \int \frac{d^2\mathbf{q}}{(2\pi^2)} e^{-i\mathbf{b}\mathbf{q}} \frac{\mathbf{q}}{q^2 + x^2 M_A^2} F_{em}(q^2 + x^2 M_A^2)$
 - $S_{abs}^2(\mathbf{b}) \cong \theta(\mathbf{b} - 2R_A)$
-
- $\frac{1}{\pi} \int d^2\mathbf{b} |\mathbf{E}(x, \mathbf{b})|^2 = \int d^2\mathbf{b} N(\omega, \mathbf{b})$
 - $d\omega_1 d\omega_2 \rightarrow dW_{\gamma\gamma} dY$

Form factor

MONOPOLE F_{em}

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

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- $^{208}\text{Pb} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}.$

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In the literature:

$$\Lambda = (0.08 - 0.09) \text{ GeV}$$

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REALISTIC F_{em}

$$F(q) = \int \frac{4\pi}{q} \rho(r) \sin(qr) r dr$$

Form factor

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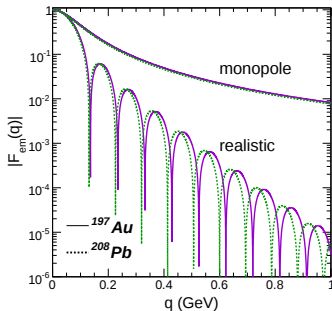
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The cross section in EPA

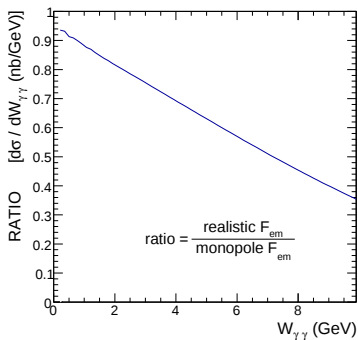
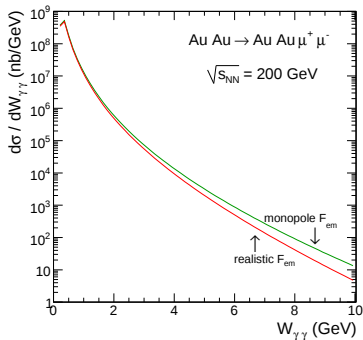
Nuclear cross section – EPA (impact parameter space)

$$\begin{aligned} \sigma(PbPb \rightarrow \pi\pi PbPb; s_{NN}) &= \\ &= \int \hat{\sigma}(\gamma\gamma \rightarrow \pi\pi; W_{\gamma\gamma}) \theta(|\mathbf{b}_1 - \mathbf{b}_2| - 2R_A) \\ &\times N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_1) 2\pi b_m db_m d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY \end{aligned}$$

The details of derivation:

Antoni Szczurek, M.K-G; Phys. Rev. **C82** (2010) 014904,
"Exclusive muon-pair productions in ultrarelativistic heavy-ion collisions: Realistic nucleus charge form factor and differential distributions"

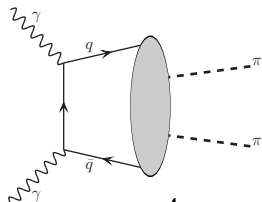
Realistic vs monopole form factor



ELEMENTARY CROSS SECTION - $\gamma\gamma \rightarrow \pi\pi$

ELEMENTARY CROSS SECTION - $\gamma\gamma \rightarrow \pi\pi$

Hand-bag model



M. Diehl, P. Kroll and C. Vogt,
Phys. Lett. **B532** (2002) 99;

M. Diehl and P. Kroll,
Phys. Lett. **B683** (2010) 165.

$$\mathcal{A}_{+-} = \mathcal{A}_{-+} = -4\pi\alpha_{em} \frac{s^2}{tu} R_{\pi\pi}(s)$$

$$R_{\pi\pi}(s) = \frac{5}{9s} a_u \left(\frac{s_0}{s}\right)^{n_u} + \frac{1}{9s} a_s \left(\frac{s_0}{s}\right)^{n_s}$$

- $s_0 = 9 \text{ GeV}^2$

- $a_u = 1.375 \text{ GeV}^2$

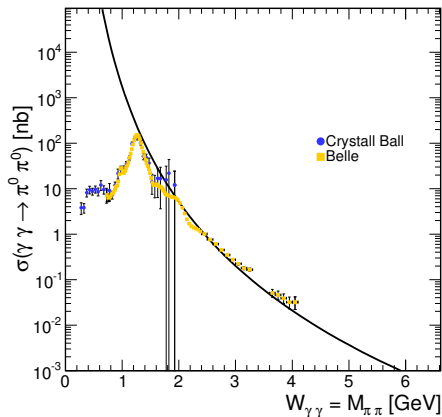
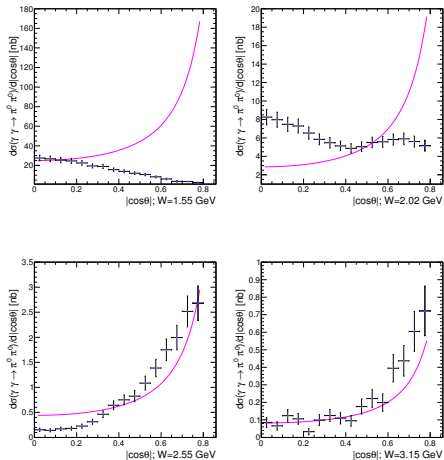
- $a_s = 0.5025 \text{ GeV}^2$

- $n_u = 0.4175$

- $n_s = 1.195$

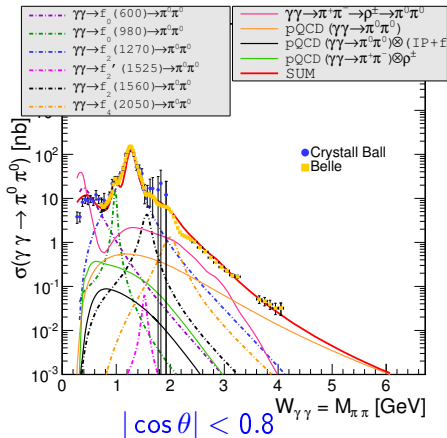
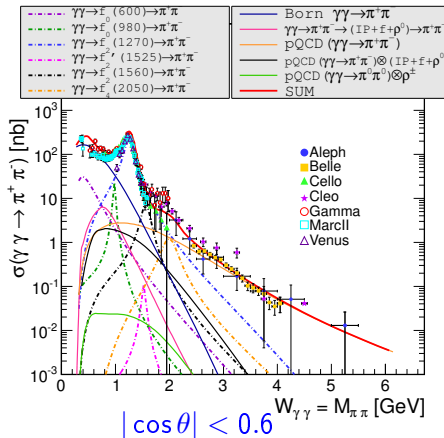
$$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-) = \frac{4\pi\alpha_{em}^2}{s} \left(\frac{\cos\theta_0}{\sin^2\theta_0} + \frac{1}{2} \ln \frac{1+\cos\theta_0}{1-\cos\theta_0} \right) |R_{\pi\pi}(s)|^2$$

Hand-bag - PREDICTIONS

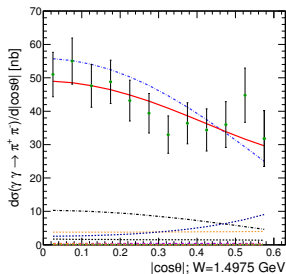
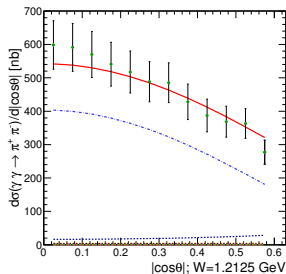
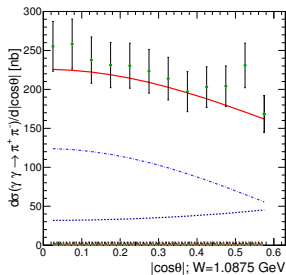
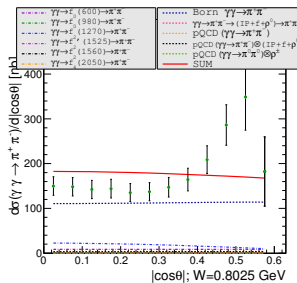


Elementary cross section for $\gamma\gamma \rightarrow \pi\pi$

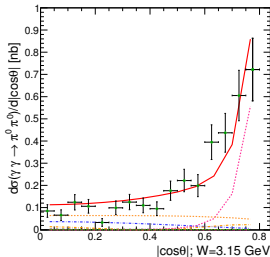
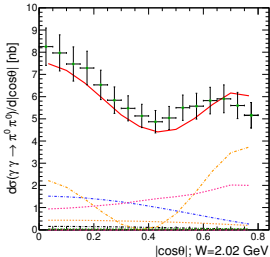
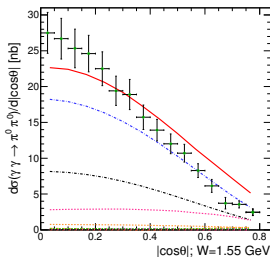
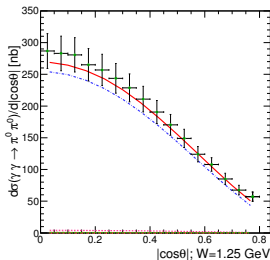
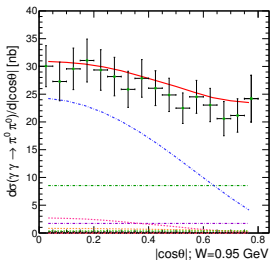
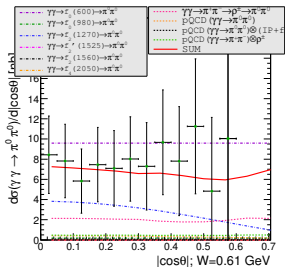
Our description



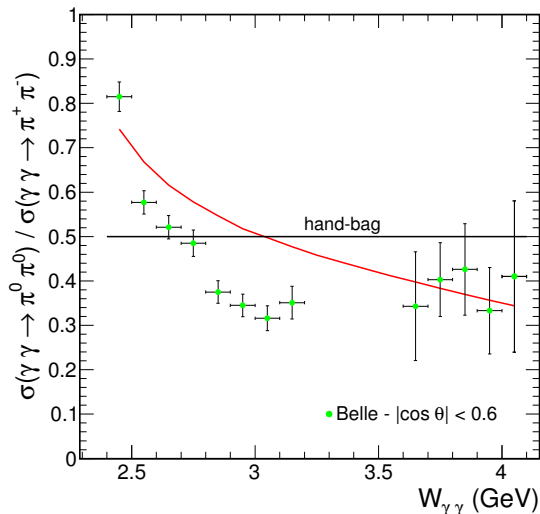
Angular Distribution - $\gamma\gamma \rightarrow \pi^+\pi^-$



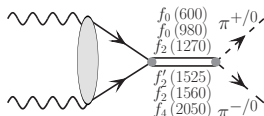
Angular Distribution - $\gamma\gamma \rightarrow \pi^+\pi^-$



our results vs hand-bag mechanism



s-channel $\gamma\gamma \rightarrow$ resonances



$$\mathcal{M}(\lambda_1, \lambda_2) = \frac{\sqrt{64\pi^2 W^2 \times 8\pi(2J+1) \left(\frac{m_R}{W}\right)^2 \Gamma_R} \Gamma_R(W)}{W^2 - m_R^2 + im_R \Gamma_R(W)}$$

$$\times \sqrt{Br(R \rightarrow \gamma\gamma) Br(R \rightarrow \pi^{+}/0 \pi^{-}/0)} \exp(i\varphi_R) \exp\left(\frac{-(W-m_R^2)^2}{\Lambda_R^2}\right)$$

$$\times \sqrt{2} \delta_{\lambda_1, \lambda_2} \begin{cases} Y_0^0; \text{ for } f_0(600), f_0(980) \\ Y_2^2; \text{ for } f_2(1270), f_2'(1525), f_2(1560) \\ Y_4^2; \text{ for } f_4(2050) \end{cases}$$

s-channel $\gamma\gamma \rightarrow$ resonances

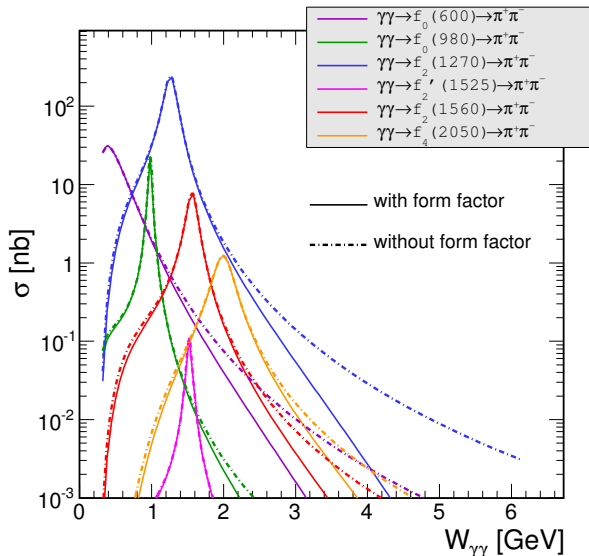
Form factor:

$$\exp\left(\frac{-(W-m_R^2)^2}{\Lambda_R^2}\right)$$

$$\Lambda_R = 2.5 \text{ GeV}$$

- $\Gamma_{f_0(600)} = 0.8 \text{ GeV}$
- $\Gamma_{f_0(980)} = 0.05 \text{ GeV}$
- $\Gamma_{f_2(1270)} = 0.185 \text{ GeV}$
- $\Gamma_{f_2'(1525)} = 0.073 \text{ GeV}$
- $\Gamma_{f_2(1560)} = 0.16 \text{ GeV}$
- $\Gamma_{f_4(2050)} = 0.3 \text{ GeV}$

$$\Gamma_R > 0.1 \text{ GeV} !$$



s-channel $\gamma\gamma \rightarrow$ resonances

$$\Gamma_R(W) = \Gamma_R \frac{\sqrt{\frac{W^2}{4} - m_\pi^2}}{\sqrt{\frac{m_R^2}{4} - m_\pi^2}} F^J(W, R)$$

Blatt-Weisskopf form factors:

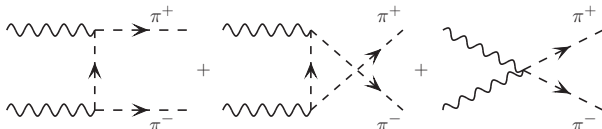
$$F^{J=0}(W, R) = 1,$$

$$F^{J=2}(W, R) = \frac{(Rp_R)^4 + 3(Rp_R)^2 + 9}{(Rp)^4 + 3(Rp)^2 + 9},$$

$$F^{J=4}(W, R) = \frac{(Rp_R)^8 + 10(Rp_R)^6 + 135(Rp_R)^4 + 1575(Rp_R)^2 + 11025}{(Rp)^8 + 10(Rp)^6 + 135(Rp)^4 + 1575(Rp)^2 + 11025}$$

- $R=5 \text{ GeV}^{-1}$

$\gamma\gamma \rightarrow \pi^+\pi^-$ continuum



$$\mathcal{M}_{\lambda_1\lambda_2}^{\pi,c}(q_1, q_2, p_{\pi^+}, p_{\pi^-}) = e^2 \sum 2g^{\mu,\nu} \varepsilon_\mu(\lambda_1) \varepsilon_\nu(\lambda_2)$$

$$\begin{aligned} \mathcal{M}_{\lambda_1\lambda_2}^{\pi,t}(q_1, q_2, p_{\pi^+}, p_{\pi^-}) &= \\ = e^2 \sum (2p_{\pi^-}^\mu - q_1^\mu) \varepsilon_\mu(q_1, \lambda_1) (2p_{\pi^+}^\nu - q_2^\nu) \varepsilon_\nu(q_2, \lambda_2) \frac{1}{t - m_\pi^2} \end{aligned}$$

$$\begin{aligned} \mathcal{M}_{\lambda_1\lambda_2}^{\pi,u}(q_1, q_2, p_{\pi^+}, p_{\pi^-}) &= \\ = e^2 \sum (2p_{\pi^+}^\mu - q_1^\mu) \varepsilon_\mu(q_1, \lambda_1) (2p_{\pi^-}^\nu - q_2^\nu) \varepsilon_\nu(q_2, \lambda_2) \frac{1}{u - m_\pi^2} \end{aligned}$$

$\gamma\gamma \rightarrow \pi^+\pi^-$ continuum

$$\mathcal{M}_{\lambda_1\lambda_2}^\pi = \left(\mathcal{M}_{\lambda_1\lambda_2}^{\pi,c} + \mathcal{M}_{\lambda_1\lambda_2}^{\pi,t} + \mathcal{M}_{\lambda_1\lambda_2}^{\pi,u} \right) \Omega(t, u, s)$$

$$\Omega(t, u, s) = \frac{F^2(t) + F^2(u)}{1 + F^2(-s)}$$

$$F(x) = \exp\left(\frac{B_{\gamma\pi}}{4}x\right)$$

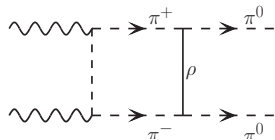
- $B_{\gamma\pi} = 4 \text{ GeV}^{-2}$

$$\gamma\gamma \rightarrow \pi^+\pi^- \rightarrow \rho^\pm \rightarrow \pi^0\pi^0$$

$$\begin{aligned} \mathcal{M}^t(\lambda_1, \lambda_2) = & \int \frac{eF(\kappa^2, k_1^2)}{\kappa_2^2 - m_\pi^2 + i\epsilon} \frac{F(\kappa_2^2, k_1^2)}{k_1^2 - m_\pi^2 + i\epsilon} \\ & \times g_{\pi\pi \rightarrow \rho} \frac{F(\kappa^2, k_2^2)}{\kappa_2^2 - m_\rho^2 + i\epsilon} g_{\pi\pi \rightarrow \rho} \frac{eF(\kappa_2^2, k_2^2)}{k_2^2 - m_\pi^2 + i\epsilon} \\ & \times (k_1^\alpha + p_{\pi^+}^\alpha) (-g_{\alpha,\beta}) (k_2^\beta + p_{\pi^-}^\beta) \\ & \times \epsilon_\mu(\lambda_1) (\kappa^\mu + k_1^\mu) \epsilon_\nu(\lambda_2) (\kappa^\nu - k_2^\nu) d\kappa_0 d\kappa_x d\kappa_y d\kappa_z \frac{1}{(2\pi)^2} \end{aligned}$$

$$F(\kappa^2, k_1^2) = \exp\left(\frac{-|\kappa^2 - m_\pi^2|}{\Lambda_{BOX}^2}\right) \exp\left(\frac{-|k_1^2 - m_\pi^2|}{\Lambda_\pi^2}\right)$$

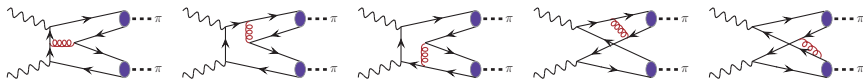
- $\Lambda_\pi = 2.7 \text{ GeV}$
- $\Lambda_{BOX} = 1.05 \text{ GeV}$



pQCD($\gamma\gamma \rightarrow \pi\pi$) [M.K-G and A.Szczurek, Phys. Lett B 700 (2011) 322]

The $\gamma\gamma \rightarrow (q\bar{q})(q\bar{q}) \rightarrow \pi\pi$ amplitude in the LO pQCD:

$$\mathcal{M}(\lambda_1, \lambda_2) = \int_0^1 dx \int_0^1 dy \phi_\pi(x, \mu_x^2) T_H^{\lambda_1 \lambda_2}(x, y, \mu^2) \phi_\pi(y, \mu_y^2) \times F_{reg}^{pQCD}(t, u)$$



- $\mu_x = \min(x, 1-x) \sqrt{s(1-z^2)}$,
 - $z = \cos \theta$,
 - $F_{reg}^{pQCD}(t, u) = \left[1 - \exp\left(\frac{t-t_m}{\Lambda_{reg}^2}\right) \right] \left[1 - \exp\left(\frac{u-u_m}{\Lambda_{reg}^2}\right) \right]$
- *A.Szczurek and J. Speth, Eur. Phys. J. A18 (2003) 445

The quark distribution amplitude of the pion

$$\phi_\pi(x, \mu^2) = \frac{f_\pi}{2\sqrt{3}} 6x(1-x) \sum_{n=0}^{\infty'} C_n^{3/2}(2x-1) a_n(\mu^2)$$

$$a_n(\mu^2) = \frac{2}{3} \frac{2n+3}{(n+1)(n+2)} \left(\frac{\alpha_s(\mu^2)}{\alpha_s(\mu_0^2)} \right)^{-\frac{C_F}{\beta_0} \left[3 + \frac{2}{(n+1)(n+2)} - 4 \sum_{k=1}^{n+1} \frac{1}{k} \right]}$$

$$\times \int_0^1 dx C_n^{3/2}(2x-1) \phi_\pi(x, \mu_0^2)$$

- $\alpha_s(\mu^2) = \frac{4\pi}{\beta_0 \ln \frac{\mu^2}{\Lambda_{QCD}^2}}$

- $\beta_0 = \frac{11}{3} C_A - \frac{2}{3} N_F$

The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

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The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both $Q^2 \rightarrow 0$ and $Q^2 \rightarrow \infty$. Our results show that to be consistent with the new BABAR data at the large Q^2 region, a broader amplitude other than the asymptotic pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter B . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting B to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

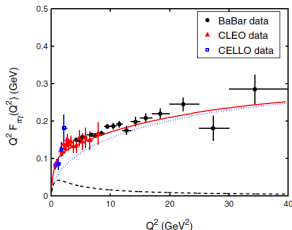


FIG. 5 (color online). $Q^2 F_{\pi\gamma}(Q^2)$ with the model wave function (3) by taking $m_q = 0.30$ GeV and $B = 0.60$. The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

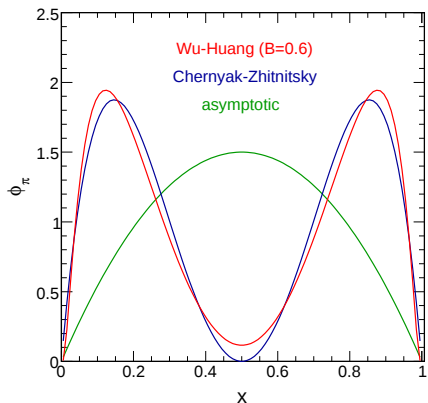
$$\begin{aligned} \phi_\pi(x, \mu_0^2)_{\text{WH}} &= \\ &= \frac{\sqrt{3} A m_q \beta}{2\sqrt{2} \pi^{3/2} f_\pi} \sqrt{x(1-x)} \\ &\times \left(1 + B \times C_2^{3/2} (2x-1) \right) \\ &\times \left(\text{erf} \left[\sqrt{\frac{m_q^2 + \mu_0^2}{8\beta^2 x(1-x)}} \right] \right. \\ &\quad \left. - \text{erf} \left[\sqrt{\frac{m_q^2}{8\beta^2 x(1-x)}} \right] \right) \end{aligned}$$

- $B = 0.6$
- $m_q = 0.3$ GeV
- $A = 16.62 \text{ GeV}^{-1}$
- $\beta = 0.745 \text{ GeV}$

The quark distribution amplitude of the pion

$$\phi_\pi(x)_{\text{cz}} = 30x(1-x)(2x-1)^2$$

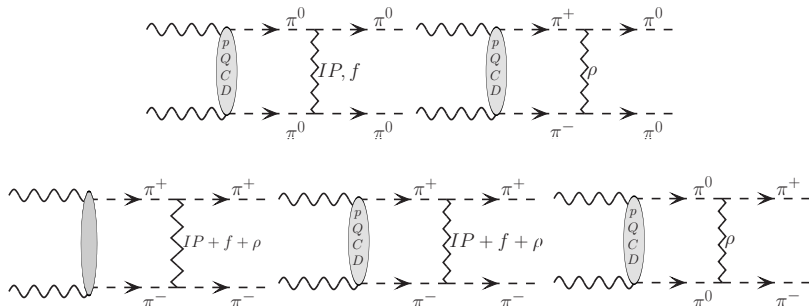
$$\phi_\pi(x)_{\text{as}} = 6x(1-x)$$



$$\begin{aligned} & \phi_\pi(x, \mu_0^2)_{\text{WH}} = \\ &= \frac{\sqrt{3} A m_q \beta}{2\sqrt{2} \pi^{3/2} f_\pi} \sqrt{x(1-x)} \\ &\times \left(1 + B \times C_2^{3/2} (2x-1) \right) \\ &\times \left(\operatorname{erf} \left[\sqrt{\frac{m_q^2 + \mu_0^2}{8\beta^2 x(1-x)}} \right] \right. \\ &\quad \left. - \operatorname{erf} \left[\sqrt{\frac{m_q^2}{8\beta^2 x(1-x)}} \right] \right) \end{aligned}$$

- $B = 0.6$
- $m_q = 0.3 \text{ GeV}$
- $A = 16.62 \text{ GeV}^{-1}$
- $\beta = 0.745 \text{ GeV}$

High energy pion-pion rescattering



$$\begin{aligned}
 \mathcal{M}_{\gamma\gamma \rightarrow \pi^+ \pi^-} &= \sum_{\alpha} \mathcal{M}_{\gamma\gamma \rightarrow \pi^+ \pi^-}^{(\alpha)} \\
 &+ \sum_{ij} \sum_{\alpha, \beta} \frac{i}{16\pi^2 s} \int d^2 \vec{k}_1 d^2 \vec{k}_2 \delta^2(\vec{k} - \vec{k}_1 - \vec{k}_2) \\
 &\times \mathcal{M}_{\gamma\gamma \rightarrow ij}^{\alpha}(s, \vec{k}_1) \mathcal{M}_{ij \rightarrow \pi^+ \pi^-}^{\beta}(s, \vec{k}_2) + (\dots)
 \end{aligned}$$

$IP + f + \rho$

$$\mathcal{M}_{IP+f+\rho}^{t/u}(\lambda_1, \lambda_2) = \sum_{X=IP, f, \rho} \left(C_X \varphi_X \left(\frac{s}{s_0} \right)^{\alpha_X(t/u)} \right) F^2(t/u)$$

$$F(t/u) = \exp\left(\frac{B}{4}t/u\right)$$

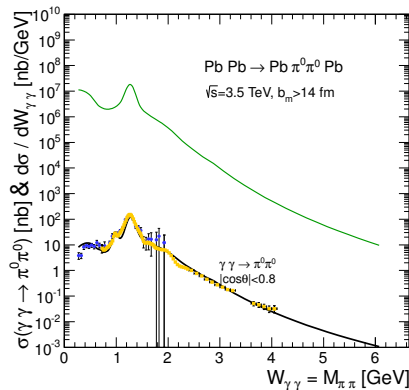
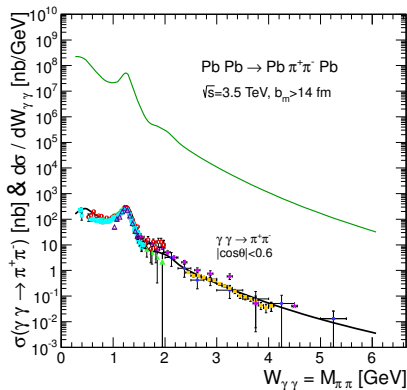
- $B=4 \text{ GeV}^{-2}$
- $s_0 = 1 \text{ GeV}^2$

X	$\alpha_X(t/u) = \alpha_X^0 + \alpha' t/u$	φ_X
IP	$1.0808 + (0.25 \text{ GeV}^{-2})t/u$	i
f	$0.5475 + (0.93 \text{ GeV}^{-2})t/u$	$\frac{-1}{\sin(\frac{\pi}{2}\alpha_f^0)} \exp\left(\frac{-i\pi}{2}\alpha_f\right)$
ρ	$0.5475 + (0.93 \text{ GeV}^{-2})t/u$	$\frac{-i}{\cos(\frac{\pi}{2}\alpha_\rho^0)} \exp\left(\frac{-i\pi}{2}\alpha_\rho\right)$

*P. Lebiedowicz and A. Szczurek, Phys. Rev. **D83** (2011) 076002

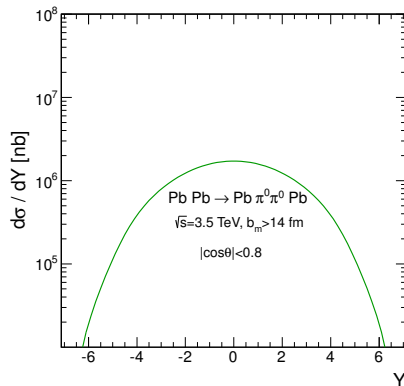
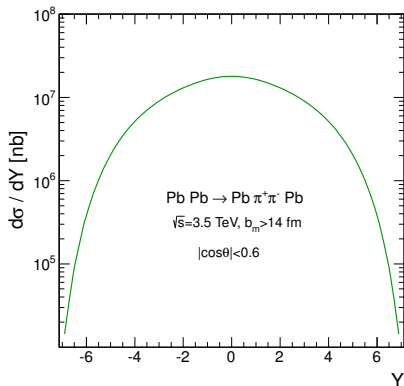
Results - NUCLEAR CROSS SECTION -

$$\frac{d\sigma}{dW_{\gamma\gamma}}$$

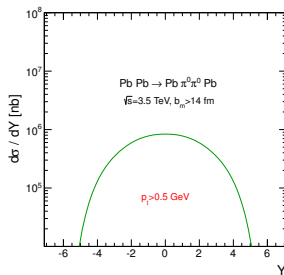
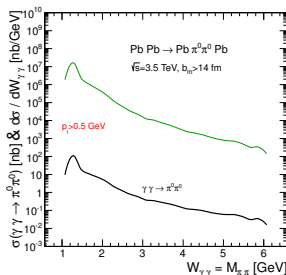
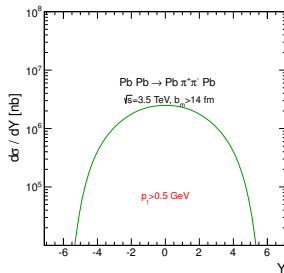
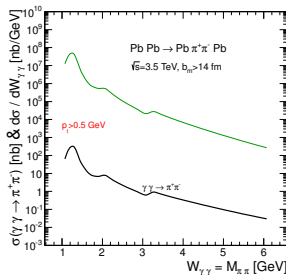


Results - NUCLEAR CROSS SECTION -

$$\frac{d\sigma}{dY}_{\pi\pi}$$



Results - $Pb + Pb \rightarrow Pb + Pb + \pi + \pi - p_t > 0.5 \text{ GeV}$



Conclusions

Elementary cross section for $\gamma\gamma \rightarrow \pi\pi$:

$$\gamma\gamma \rightarrow \pi^+\pi^-$$

- resonances
- $\gamma\gamma \rightarrow \pi^+\pi^- \rightarrow (IP + f + \rho^0) \rightarrow \pi^+\pi^-$
- $pQCD(\gamma\gamma \rightarrow \pi^+\pi^-)$
- $pQCD(\gamma\gamma \rightarrow \pi^+\pi^-) \otimes (IP + f + \rho^0)$
- $pQCD(\gamma\gamma \rightarrow \pi^0\pi^0) \otimes \rho^\pm$
- $\gamma\gamma \rightarrow \pi^+\pi^-$

$$\gamma\gamma \rightarrow \pi^0\pi^0$$

- resonances
- $\gamma\gamma \rightarrow \pi^+\pi^- \rightarrow \rho^\pm \rightarrow \pi^0\pi^0$
- $pQCD(\gamma\gamma \rightarrow \pi^0\pi^0)$
- $pQCD(\gamma\gamma \rightarrow \pi^0\pi^0) \otimes (IP + f)$
- $pQCD(\gamma\gamma \rightarrow \pi^+\pi^-) \otimes \rho^\pm$

Conclusions

Nuclear cross section:

$\sqrt{s} = 3.5$ TeV + peripheral collisions + realistic form factor

$PbPb \rightarrow PbPb\pi^+\pi^-:$		112 mb
$PbPb \rightarrow PbPb\pi^+\pi^-$	$\& p_t > 0.5$ GeV:	14 mb
$PbPb \rightarrow PbPb\pi^0\pi^0:$		10 mb
$PbPb \rightarrow PbPb\pi^0\pi^0$	$\& p_t > 0.5$ GeV:	5 mb

Background to the exclusive ρ^0 production

Conclusions

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Background to the exclusive ρ^0 production

Thank You For Attention