Dipole model analysis of $F_2^{c\overline{c}}$ **and PDFs from the new HERA data**

Agnieszka Łuszczak

Krakow University of Technology, Poland

in collaboration with Henri Kowalski and Sasha Glazov

MESON2012, May 31, 2012

Motivation : Investigation of the gluon density with dipole model, as an alternative to the PDF approach. Prefered choice : BGK dipole model, which has very similar physics interpretation as PDFs, i.e. DGLAP evolution in the *kt* factorization scheme (in contrast to the collinear factorization for PDFs).

- Dipole model approach
- GBW and BGK parametrization of dipole cross section
- Results of the fits
 - Fits to $F_2^{c\overline{c}}$ function
 - Fits to σ_r with different valence quarks contributions
 - Fits to σ_r from HERAFitter package
- Conclusions

Dipole picture of DIS at small x in the proton rest frame



r - dipole size

z - longitudinal momentum fraction of the quark/antiquark

Factorization: dipole formation + dipole interaction

$$\sigma^{\gamma p} = \frac{4\pi^2 \alpha_{em}}{Q^2} F_2 = \sum_f \int d^2 r \int_0^1 dz \, |\Psi^{\gamma}(r, z, Q^2, m_f)|^2 \, \hat{\sigma}(r, x)$$

Dipole-proton interaction
$$\hat{\sigma}(r,x) = \sigma_0 \left(1 - \exp\{-\hat{r}^2\}\right) \qquad \hat{r} = r/R_s(x)$$

Dipole cross section with GBW parametrization

• GBW (Golec-Biernat, Wüsthoff) parametrization $\hat{\sigma}(r,x) = \sigma_0 \left(1 - \exp(-r^2/R_s^2)\right), \qquad R_s^2 = 4 \cdot \left(x/x_0\right)^{\lambda} \, \mathrm{GeV}^2$

The dipole scattering amplitude in such a case reads

$$\hat{N}(\mathbf{r}, \mathbf{b}, x) = \theta(b_0 - b) \left(1 - \exp(-r^2/R_s^2)\right)$$

where

$$\hat{\sigma}(r,x) = 2 \int d^2 b \, \hat{N}(\mathbf{r},\mathbf{b},x)$$

Parameters b_0 , x_0 and λ from fits of \hat{N} to F_2 data

 $\lambda = 0.288$ $x_0 = 4 \cdot 10^{-5}$ $2\pi b_0^2 = \sigma_0 = 29 \text{ mb}$

Dipole cross section with BGK parametrization

BGK (Bartels-Golec-Kowalski) parametrization

 $\hat{\sigma}(r,x) = \sigma_0 \left\{ 1 - \exp\left[-\pi^2 r^2 \alpha_s(\mu^2) x g(x,\mu^2) / (3\sigma_0)\right] \right\}$

- \square R_s^2 is replacing by a gluon density with explicit DGLAP evolution
- $\mu^2 = C/r^2 + \mu_0^2$ is the scale of the gluon density
- gluon density is evolved according to the (LO) DGLAP equation

$$xg(x,\mu_0^2) = A_g x^{-\lambda_g} (1-x)^{C_g}$$

J The $q\overline{q}$ components from T and L polarised photons are given by

$$\begin{split} F_T^{(q\overline{q})} &= \frac{3Q^4}{64\pi^4} \sum_f e_f^2 \int_{z_f}^{1/2} dz \, z(1-z) \\ &\times \quad \left\{ \left[z^2 + (1-z)^2 \right] Q_f^2 \, \phi_1^2 + \, m_f^2 \, \phi_0^2 \right\} \\ F_L^{(q\overline{q})} &= \frac{3Q^6}{16\pi^4} \, \sum_f e_f^2 \int_{z_f}^{1/2} dz \, z^3 (1-z)^3 \, \phi_0^2 \end{split}$$

The functions ϕ_i take the following form for i = 0, 1

$$\phi_i = \int_0^\infty dr r K_i(Q_f r) J_i(k_f r) \,\hat{\sigma}(r, x)$$

$$x = \frac{Q^2}{Q^2 + W^2}$$

Charm structure functions in dipole models

Standard dipole model formula with $m_c = 1.4 \text{ GeV}$ and $e_c = 2/3$

$$F_T^{(c\overline{c})} = \frac{3Q^4 e_c^2}{64\pi^4} \int_{z_c}^{1/2} dz \, z(1-z)$$
$$\times \quad \left\{ \left[z^2 + (1-z)^2 \right] Q_c^2 \, \phi_1^2 + m_c^2 \, \phi_0^2 \right\}$$

with
$$z_c = (1 - \sqrt{1 - 4m_c^2/M^2})/2$$

Solution For the heavy quark contributions we modyfied x in $\hat{\sigma}(r, x)$

$$x \to x(1 + \frac{4m_f^2}{Q^2}) = \frac{Q^2 + 4m_f^2}{Q^2 + W^2}$$

Dipole model BGK fit with charm quark contribution

1.1 Pure dipole fit for σ_r with $m_{ch} = 1.3$ GeV, $m_{ud} = 0.03$ GeV, E = 460, 575 and 920 GeV.

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 0.25$	483	754.81	3.089	-0.059	0.959	1.56
2	H1 and ZEUS	$Q^2 \ge 1.5$	402	402.27	2.276	0.062	1.719	1.0
3	H1 and ZEUS	$Q^2 \ge 3.5$	356	343.02	2.159	0.085	2.016	0.96
4	H1 and ZEUS	$Q^2 \ge 8.5$	287	229.79	2.147	0.085	1.99	0.80

1.2 Pure dipole fit for σ_r with $m_{ch} = 1.4 \text{ GeV}$, $m_{ud} = 0.03 \text{ GeV}$, E = 460, 575and 920 GeV.

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 0.25$	483	769.43	3.130	-0.059	0.954	1.59
2	H1 and ZEUS	$Q^2 \ge 1.5$	402	401.36	2.281	0.065	1.723	0.99
3	H1 and ZEUS	$Q^2 \ge 3.5$	356	344.27	2.175	0.086	1.994	0.97
4	H1 and ZEUS	$Q^2 \ge 8.5$	287	229.76	2.167	0.084	1.944	0.80

Results of the Fits

Dipole model BGK fit for $F_2^{c\overline{c}}$

1.7 Charm fit for $F_2^{c\overline{c}}$ function, $m_{ch} = 1.4 \text{ GeV}, m_{ud} = 0.03 \text{ GeV}.$

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 2.5$	41	32.36	4.917	-0.349	0.415	0.89

1.8 Charm fit for $F_2^{c\overline{c}}$ function, $m_{ch} = 1.3 \text{ GeV}, m_{ud} = 0.03 \text{ GeV}.$

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 2.5$	41	31.17	5.117	-0.231	0.221	0.93

Predictions for $F_2^{c\overline{c}}$ from fits



ZEUS and H1 Data

Results of the Fits

Dipole model BGK fit with different valence quarks contributions

1.4 Dipole fit with HERAPDF valence - quark contribution added to σ_r , $m_{ch} = 1.4 \text{ GeV}, m_{ud} = 0.03 \text{ GeV}, E = 820, 920 \text{ GeV}.$

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 3.5$	177	229.93	1.446	0.109	1.341	1.29
2	H1 and ZEUS	$Q^2 \ge 8.5$	138	155.54	1.469	0.101	1.264	1.12

1.6 Dipole fit with MSTW valence - quark contribution added to σ_r , $m_{ch} = 1.4 \text{ GeV}, m_{ud} = 0.03 \text{ GeV}, E = 820, 920 \text{ GeV}.$

No	Data	Q^2	Npoints	χ^2	A_g	λ_g	μ_0	$\chi^2/N points$
1	H1 and ZEUS	$Q^2 \ge 3.5$	177	281.06	2.602	-0.050	0.785	1.58
2	H1 and ZEUS	$Q^2 \ge 8.5$	138	208.48	2.599	-0.050	0.785	1.51

Dipole model BGK fit without valence quarks

1.1 Dipole model BGK fit without valence quarks for σ_r for H1ZEUS-NC-(e+p) and H1ZEUS-NC-(e-p) data in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 0.01$.

No	Q^2	HF Scheme	σ_0	A_g	λ_g	cBGK	eBGK	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	40.43	1.596	-0.249	1.529	0.401	197	214.46	1.10
2	$Q^2 \ge 3.5$	ACOT Full	40.43	1.596	-0.249	1.529	0.401	197	214.46	1.10
3	$Q^2 \ge 8.5$	RT	32.48	1.691	-0.256	1.463	0.155	156	125.10	0.80
4	$Q^2 \ge 8.5$	ACOT Full	32.48	1.691	-0.256	1.463	0.155	156	125.10	0.80

1.2 Dipole model BGK fit without valence quarks for σ_r for H1ZEUS-NC-(e+p) and H1ZEUS-NC-(e-p) and H1-LowEp-460-575 data in the range $Q^2 \geq 3.5$ and $Q^2 \geq 8.5$ and $x \leq 0.01$.

No	Q^2	HF Scheme	σ_0	A_g	λ_g	cBGK	eBGK	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	38.67	1.593	-0.254	1.336	0.349	318	365.19	1.15
2	$Q^2 \ge 3.5$	ACOT Full	38.67	1.593	-0.254	1.336	0.349	318	365.19	1.15
3	$Q^2 \ge 8.5$	RT	31.47	1.74	-0.255	1.556	-0.542	249	224.48	0.90
4	$Q^2 \ge 8.5$	ACOT Full	31.47	1.74	-0.255	1.556	-0.542	249	224.48	0.90

HERAPDF fit with valence quarks

1.3 HERAPDF fit with valence quarks for σ_r for H1ZEUS-NC-(e+p), H1ZEUS-NC-(e-p) data in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 1.0$.

No	Q^2	HF Scheme	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	511	518.06	1.01
2	$Q^2 \ge 3.5$	ACOT Full	511	501.67	0.98
3	$Q^2 \ge 8.5$	RT	469	414.70	0.88
4	$Q^2 \ge 8.5$	ACOT Full	469	416.66	0.88

1.4 HERAPDF fit with valence quarks for σ_r for H1ZEUS-NC-(e+p), H1ZEUS-NC-(e-p) data in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 0.01$.

No	Q^2	HF Scheme	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	197	220.64	1.12
2	$Q^2 \ge 3.5$	ACOT Full	197	206.85	1.05
3	$Q^2 \ge 8.5$	RT	156	131.04	0.84
4	$Q^2 \ge 8.5$	ACOT Full	156	131.04	0.84

HERAPDF fit with valence quarks

1.5 HERAPDF fit with valence quarks for σ_r for H1ZEUS-NC-(e+p), H1ZEUS-NC-(e-p), H1ZEUS-CC-(e-p), H1ZEUS-CC-(e+p) data in the range $Q^2 \geq 3.5$ and $Q^2 \geq 8.5$ and $x \leq 1.0$.

No	Q^2	HF Scheme	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	579	575.08	0.99
2	$Q^2 \ge 3.5$	ACOT Full	579	560.01	0.97
3	$Q^2 \ge 8.5$	RT	537	468.34	0.87
4	$Q^2 \ge 8.5$	ACOT Full	537	474.78	0.88

1.6 Parameters are taken from fit nb.(1.5) in all region of x. Results with valence quarks for σ_r for H1ZEUS-NC-(e+p), H1ZEUS-NC-(e-p), H1ZEUS-CC-(e+p) data in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 0.01$.

No	Q^2	HF Scheme	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	256	270.75	1.06
2	$Q^2 \ge 3.5$	ACOT Full	256	327.58	1.28
3	$Q^2 \ge 8.5$	RT	217	193.31	0.89
4	$Q^2 \ge 8.5$	ACOT Full	217	200.08	0.92

HERAPDF fit with valence quarks

1.7 HERAPDF fit with valence quarks for σ_r for H1ZEUS-NC-(e+p), H1ZEUS-NC-(e-p), H1ZEUS-CC-(e-p), H1ZEUS-CC-(e+p) data and H1-LowEp-460-575 data in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 1.0$.

No	Q^2	HF Scheme	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	703	749.92	1.07
2	$Q^2 \ge 3.5$	ACOT Full	703	704.44	1.00
3	$Q^2 \ge 8.5$	RT	631	574.62	0.91
4	$Q^2 \ge 8.5$	ACOT Full	631	567.90	0.90

Dipole model BGK fit with valence quarks

1.8 Dipole model BGK fit with valence quarks for σ_r for H1ZEUS-NC-(e+p) in the range $Q^2 \ge 3.5$ and $Q^2 \ge 8.5$ and $x \le 0.01$.

No	Q^2	HF Scheme	σ_0	A_g	λ_g	cBGK	eBGK	Np	χ^2	χ^2/Np
1	$Q^2 \ge 3.5$	RT	37.401	3.345	0.030	28.60	31.68	171	232.53	1.36
2	$Q^2 \ge 3.5$	ACOT Full	37.49	3.393	0.042	32.65	36.46	171	233.82	1.37

Comparison with HERA data

NC cross section HERA-I H1-ZEUS combined e+p.

- output3.5RT-3f

1.4 1.2 0.8	Q ² = 3.5 GeV ²	$Q^2 = 4.5 \text{ GeV}^2$	$Q^2 = 6.5 \text{ GeV}^2$	Q ² = 8.5 GeV ²	$Q^2 = 10.0 \text{ GeV}^2$	Q ² = 12 GeV ²
0.4	χ^2 / npts = 33.8 / 13	χ^2 / npts = 23.5 / 12	χ^2 / npts = 20.6 / 14	χ^2 / npts = 11.3 / 12	χ² / npts = 7.8 / 8	χ^2 / npts = 4.6 / 11
1.4 1.2 1.2 1 1.2 1 1 1 1 1 1 1 1 1 1 1 1 1	I^{Tr}_{r} Q ² = 15 GeV ²	^E Q ² = 18 GeV ²	$\mathbf{L}_{\mathbf{T}} \mathbf{Q}^2 = 22 \mathrm{GeV}^2$	$\mathbf{P}_{\mathbf{Q}^2} = 27 \mathrm{GeV}^2$	$\mathbf{Q}^2 = 35 \mathrm{GeV}^2$	₹ Q ² = 45 GeV ²
0.6	χ² / npts = 16.0 / 11	χ² / npts = 3.8 / 10	χ² / npts = 7.4 / 7	χ² / npts = 5.1 / 11	χ² / npts = 11.2 / 8	χ² / npts = 7.9 / 8
1.4 1.2 1.2 0.8	$Q^2 = 60 \text{ GeV}^2$	$Q^{2} = 70 \text{ GeV}^{2}$	$I_{Q^2} = 90 \text{ GeV}^2$	^I Q ² = 120 GeV ²	Q ² = 150 GeV ²	Q ² = 200 GeV ²
0.4	χ^2 / npts = 9.7 / 6	χ² / npts = 10.7 / 5	χ^2 / npts = 12.1 / 6	χ^2 / npts = 1.5 / 7	χ^2 / npts = 4.2 / 5	χ^2 / npts = 7.3 / 6
1.4 1.2 1.2 0.8	Q ² = 250 GeV ² ■	Q ² = 300 GeV ² ⊒	Q ² = 400 GeV ² ±	Q² = 500 GeV² ⊈	Q² = 650 GeV² ₤	
0.4	χ^{2} / npts = 5.3 / 4	χ^2 / npts = 1.3 / 5	χ² / npts = 2.6 / 3	χ² / npts = 1.0 / 3	χ² / npts = 0.8 / 2	

Summary

- BGK dipole model describe reasonable well the recent data from HERA for σ_r and $F_2^{c\overline{c}}$ function derived from D^* mesons.
- The treatment of the effects related to the charm quark contribution, is an important issue in the determination of parton distribution functions (PDFs).
- The valence quarks contributions in the region of small x < 0.01 needs refinement.
- Work in progress on BGK dipole model with valence quarks.